

Date: 25/09/19

# LECTURE NO 1

## ELECTRICAL MEASUREMENT INSTRUMENTATION

Course Outlines:-

Principle, Operation working and construction of Different Analog and Digital Meters.

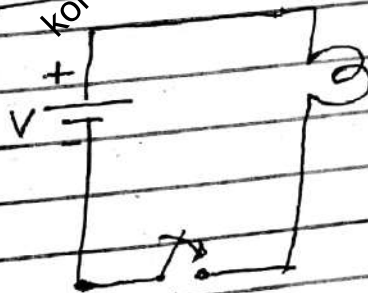
• Oscilloscope and its Measurements.

• Recording Instruments and signal generators.

• Transducers.

OBE:

Electrical:

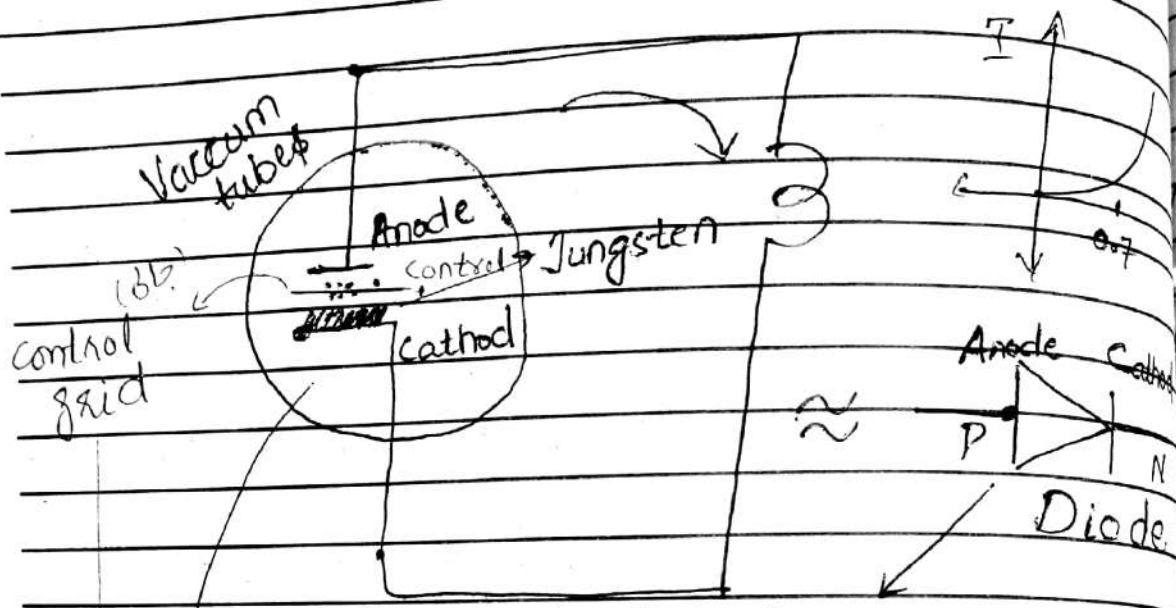


Electronics: If Bulb is control with remote is called electronics.

Vacuum Tube:

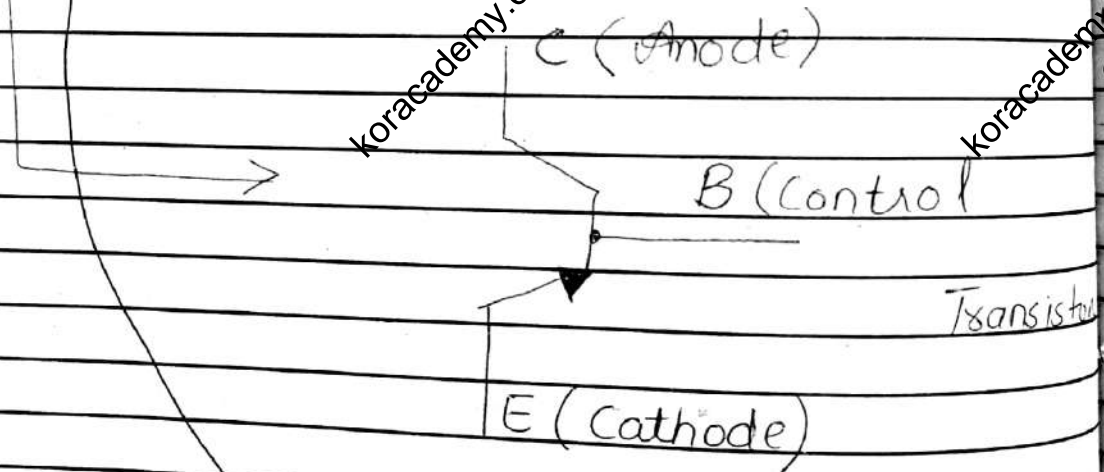
High work ftn: A metal is called of high work ftn if less amount of heat is require to free of outer es.

Jungsten is of high work ftn.



Thermionic Emission

These two are Equivalent



There is a non-uniform flow of  $e^-$  which produces noise.

To measure = to determine the magnitude or extend or degree of the condition of some system in terms of standard

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All the natural phenomena follow mathematical models. So can be mathematical modelled.

Bernoulli Equation is mathematical model of fluid natural fluid flow.  
→ e.g. Blinking of Eye and breathing.

Measuring Meter: Instrument used to indicate or record measured value.

### Instrument

- 1) Sensing
- 2) Detecting
- 3) Measuring
- 4) Recording
- 5) Controlling
- 6) Communicating.

SIR FAROOQ:

Measured Value is the value calculated using a measurement system/instrument.

True value is the value calculated from the rated values.  
rated (given)



### Accuracy Vs Precision:-

Accuracy is define as degree of value closeness of the measured value with true value is known as accuracy.

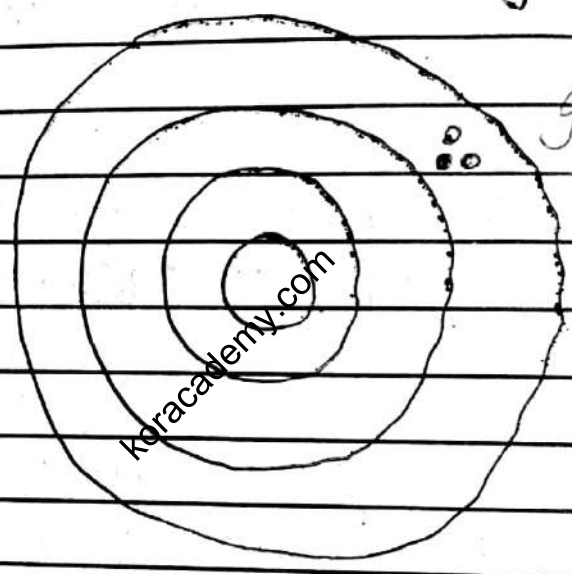
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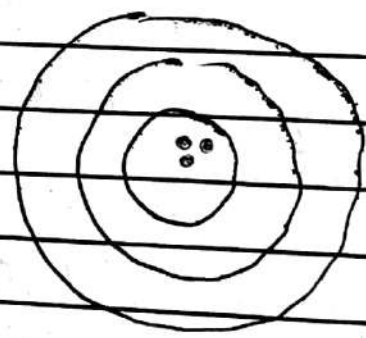
If Actual = True value  
value  
the Accuracy is 100%

Precision  
Degree of closeness of  
measured values among themselves

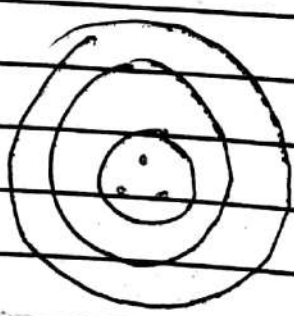
Bird Eye  
target



Inaccurate &  
precised



Accurate &  
precised



Accurate but not  
precised.

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Sensitivity: The ratio of change in output signal/response of system to change of input variable

$$S = \frac{\Delta \text{output}}{\Delta \text{input}}$$

Input  $\rightarrow$  pressure  $\rightarrow$  0 - 100 PSI  
output  $\rightarrow$  0 - 5V

PSI  $\rightarrow$  Pound per square inch.

$$S = \frac{100 \text{ PSI}}{5 \text{ V}} = \frac{1 \text{ V}}{20 \text{ PSI}}$$

Resolution:-

Smallest change in the input that can be detected.

100.00      100.001

Resolution is .01

0.006  
its resolution is .05  
and if it can round off then

$\rightarrow$  100.01

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SIGNIFICANT FIGURES:-

1) Any non-zero digit is significant figure.

Ex	Number	# of Sig fig
1) 17	17	2
2) 132.856	132.856	6
2) Any zero in between two non zeros is a sig. figure	101	3
	2,000,009	7

3) Any zero before a non zero is not a significant figure	0.5	1
	0.000305	3

4) Any zero after non-zeros are not sig figure iff the given number has no decimal point	5000	1
	Eg 5000m = 5Km or $5 \times 10^3$	

5) Any zero after non zero are significant fig if given number has decimal point	10.000	4
	5000̄	4
	5̄000	2
	50̄00	3

If there is decimal point in the number zeros after non zeros is sig.	370.	$3.70 \times 10^2$
	0.003205300	7

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GMP

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## Addition and Subtraction of sig. figure:-

One trillion 2 billions Nine thousand

$$\begin{array}{r} 2325 \cdot 2358 \\ \hline \end{array}$$

Diagram showing place values for 2325 and 2358:

- 2325: 1000's, 200's, 10's
- 2358: 10<sup>th</sup>, 1000<sup>th</sup>, 10,000<sup>th</sup>, 100<sup>th</sup>

2) Math first sig figs after.

$N_1 \rightarrow$  more accurate

$N_2 \rightarrow$  less accurate

$N_3 \rightarrow$  less accurate.

a) If both numbers has decimal point

$$\begin{array}{r} 150.0 \rightarrow 1 \text{ digit after decimal} \\ + \quad 0.702 \rightarrow 3 \text{ digit after decimal} \\ \hline 150.702 \end{array}$$

So Answer should have 1 digit after decimal.

$$150.7$$

No of sig figs & Accuracy

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$$0.854 \rightarrow 3 \text{ad}$$

$$- 0.0594 \rightarrow 4 \text{ad}$$

$$\underline{0.7946}$$

So answer will have three digit after decimal.

$$\boxed{0.796}$$

$$0.7996 \rightarrow 0.800$$

Round-off.

b) If one digit has decimal point & the other number has no decimal pt

$$4.51$$

3

$$\underline{7.51}$$

Ans  $\Rightarrow$  1's

8 (after round-off)



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$$\begin{array}{r}
 12,000 \quad \rightarrow 1000 \\
 3,500 \quad \rightarrow 100's \\
 \hline
 7,500 \quad \rightarrow \text{Ans}
 \end{array}$$

Ans  $\Rightarrow$  1000's  $\rightarrow$  8000

Last Sig fig  $\rightarrow$  position  $\rightarrow$  highest position  
?  $\in$  3000

Answer should not have significant figure after highest position (1000's)

Example:-

$$\begin{array}{r}
 500.0 \quad \rightarrow 10^{\text{th}} \\
 \leftarrow 90 \quad 10's \\
 \hline
 410.0 \\
 \downarrow \\
 \boxed{410}
 \end{array}$$

$$\begin{array}{r}
 500 \\
 -90 \\
 \hline
 410 \\
 \downarrow \\
 \boxed{400}
 \end{array}$$

$$\begin{array}{r}
 12,000 \\
 + 3,500 \\
 \hline
 15,500 \\
 \text{Ans } 16,000 \quad \text{Ans}
 \end{array}$$

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## Multiplication & Division:-

1) Math first

$$\begin{array}{r} 815.991 \rightarrow (6SF) \\ 324.6 \rightarrow (4SF) \end{array}$$

$$264,870.6786$$

$$\text{Ans} \Rightarrow S.F = 4$$

$$264,900$$

$$\begin{array}{r} 22 \\ 3 \\ \hline 36 \end{array}$$

$$\text{Ans} \Rightarrow 40$$

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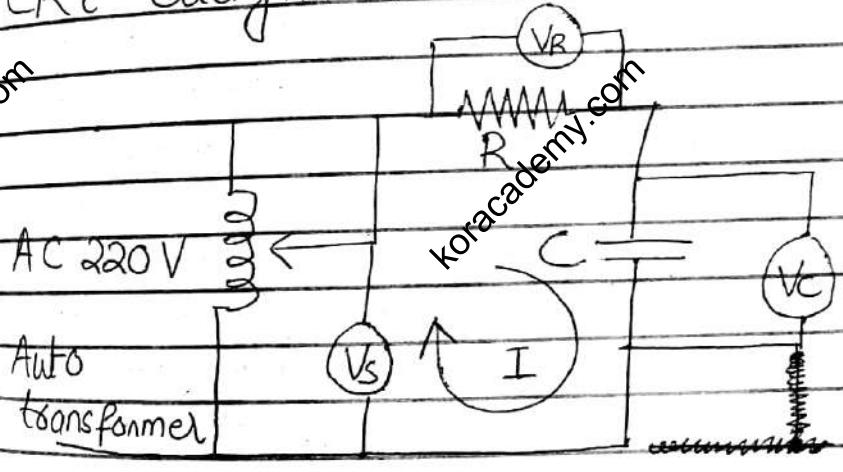
### LAB # 01 :-

To find the unknown capacitance using three voltmeters method

Apparatus:-

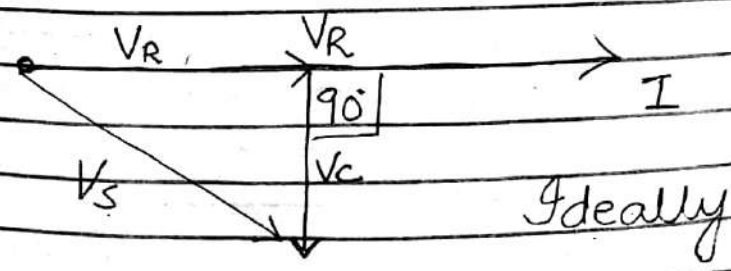
Auto transformer, rheostat, voltmeter, capacitor and wires

CKT diagram:-



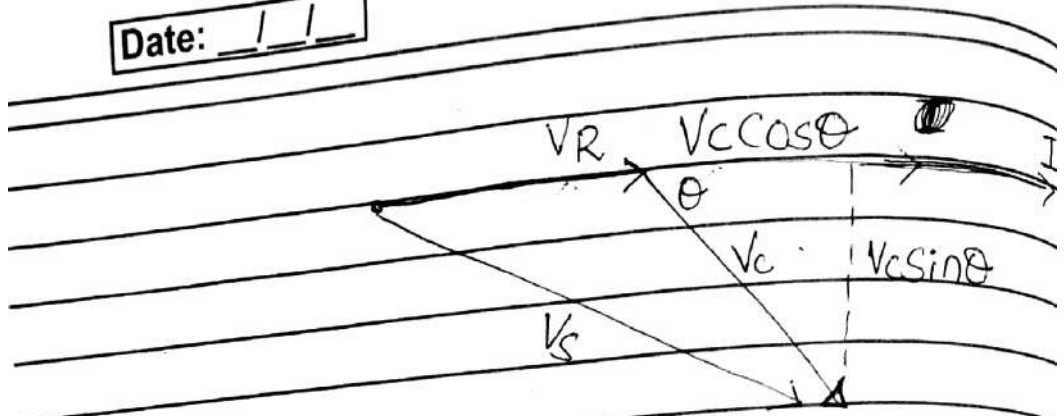
Applying KVL

$$V_s = V_R + V_C \quad (\text{Phasor sum})$$



Practically there will be some resistance of capacitor

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$$V_C \sin \theta = I \cdot X_C \quad \text{--- (A)}$$

$$V_R = I \cdot R \Rightarrow I = \frac{V_R}{R}$$

$$X_C = \frac{1}{\omega C}$$

$$V_C \sin \theta = \frac{V_R}{R} \cdot \frac{1}{2\pi f C}$$

$$C = \frac{V_R}{V_C \sin \theta \cdot R \cdot 2\pi f}$$

S.No	V <sub>s</sub>	V <sub>R</sub>	V <sub>C</sub>	C	θ	E <sub>Mon</sub>
1	100V	60V	40V		85°	

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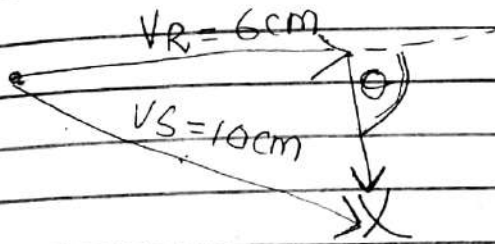
Scale:  $10V = 1cm$

$100V = 10cm$

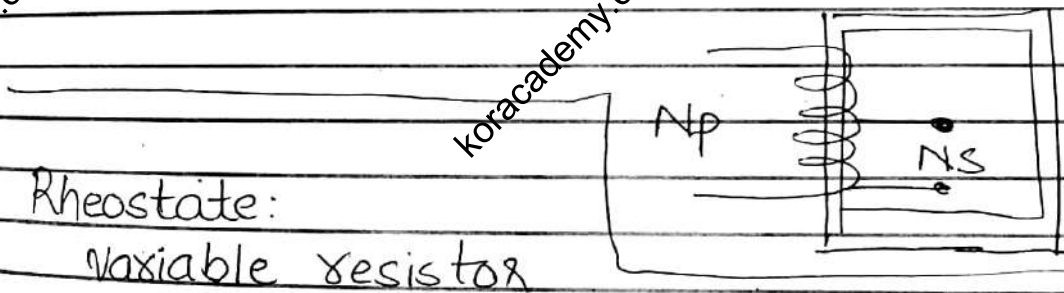
$60V = 6cm$

$40V = 4cm$

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Auto transformer has one winding & a portion of which is use for primary & secondary. It can step up and step down the given voltage.



Rheostate:

variable resistor

$Error = Measured\ value - True\ value$

Limiting Error or Relative Static Error:  $\Delta$

$$\% L.E \text{ or } \% R.S.E = \frac{Error}{True\ value} \times 100$$

$$Accuracy = 100 - \% L.E / R.S.E$$

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# LECTURE # 2

If we take many readings from the same instruments and there is no change in reading so we called this instrument as precise.

Precision is composed of two characteristics:

- 1) Conformity
- 2) the number of significant figures to which a measurement may be made

①	2
②	2.25
③	2.257
④	2.2578

Significant figs



$$\text{Error} = x_m - x_T$$

Gross Error = Human Error.

Through proper training of operator gross error will reduce.

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Random Error: Random Error are those errors due to unknown reasons.

100.00V  
100.01V

Random Error

We can reduce this error by taking multiple readings.

Statistical Error:-

Statistical Analysis:-

1) Arithmetic Mean:

$x_1, x_2, x_3, x_4, \dots, x_n$

$$\bar{x} = \frac{x_1 + x_2 + x_3 + x_4 + \dots + x_n}{n}$$

This may be the most probable value of the measured value.

2) Deviation from the mean:-

$$d_1 = x_1 - \bar{x}, \quad d_2 = x_2 - \bar{x}$$

$$d_n = x_n - \bar{x}$$

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Exple: 2, 4, 3, 3, 2

$$\bar{x} = 2.8$$

$$d_1 = -0.8 \quad d_2 = 1.2$$

$$d_3 = 0.2 \quad d_4 = 0.2$$

$$d_5 = -0.8$$

3) Average Deviation :-

$$D = \frac{|d_1| + |d_2| + |d_3| + \dots + |d_n|}{n}$$

$$D = \frac{0.8 + 1.2 + 0.2 + 0.2 + 0.8}{5} = 0.64$$

Sum of deviations will be zero. Therefore we take mode.

4) Standard Deviation :-

It is define as

RMS Deviation.

$$\sigma = \sqrt{\frac{d_1^2 + d_2^2 + d_3^2 + \dots + d_n^2}{N}}$$

$$d_1 = x_1 - \mu$$

$$d_2 = x_2 - \mu$$

Population SD

$$\sigma = \sqrt{\frac{d_1^2 + d_2^2 + d_3^2 + \dots + d_n^2}{n-1}}$$

Sample S.D



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$$d_1 = x_1 - \bar{x}$$

$$d_2 = x_2 - \bar{x}$$

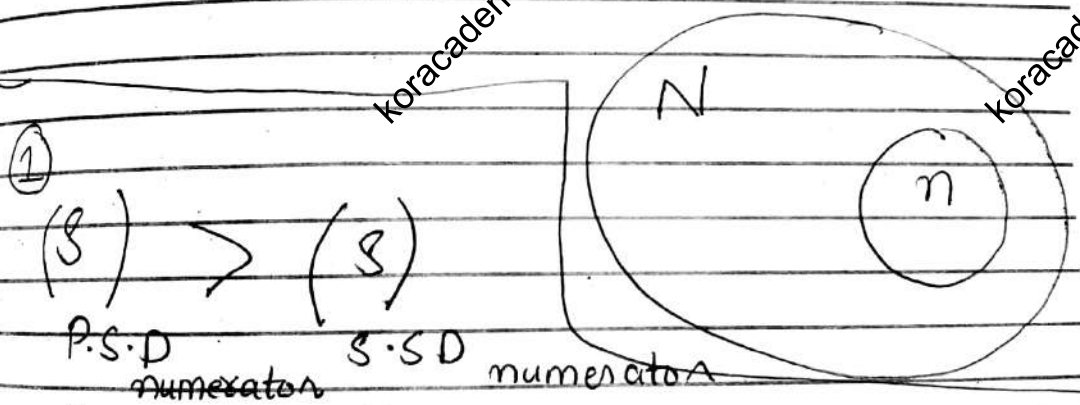
$\bar{x}$  = Estimating mean.

Parameter	Statistic
mean $\mu$	$\bar{x}$
$\mu = \frac{\sum_{i=1}^N x_i}{N}$	$\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$

→ To measure height of students of UET

→ To measure height of each & everyone.

→ To measure height of 50 students of every campus (sample)



therefore reduce denominator of one as  $(S)_{P.S.D} = (S)_{S.S.D}$

② Degree of Freedom =  $n$

Degree of Freedom =  $n - 1$

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$$\mu = 7$$

$i$	$x_i$	$d_i = x_i - \mu$
1	9	2
2	4	-3
3	?	?

$$\bar{x} = 8$$

$i$	$x_i$	$d_i = x_i - \bar{x}$
1	9	1
2	4	-4
3	11	? + 3

→ Degree of freedom =  $n$   
we cannot insert any value.

$$x_1, x_2, x_3, x_4, \dots, x_{1000}$$

10

It is not necessary mean of all population is 10.

$$\text{Degree of freedom} = n - 1$$

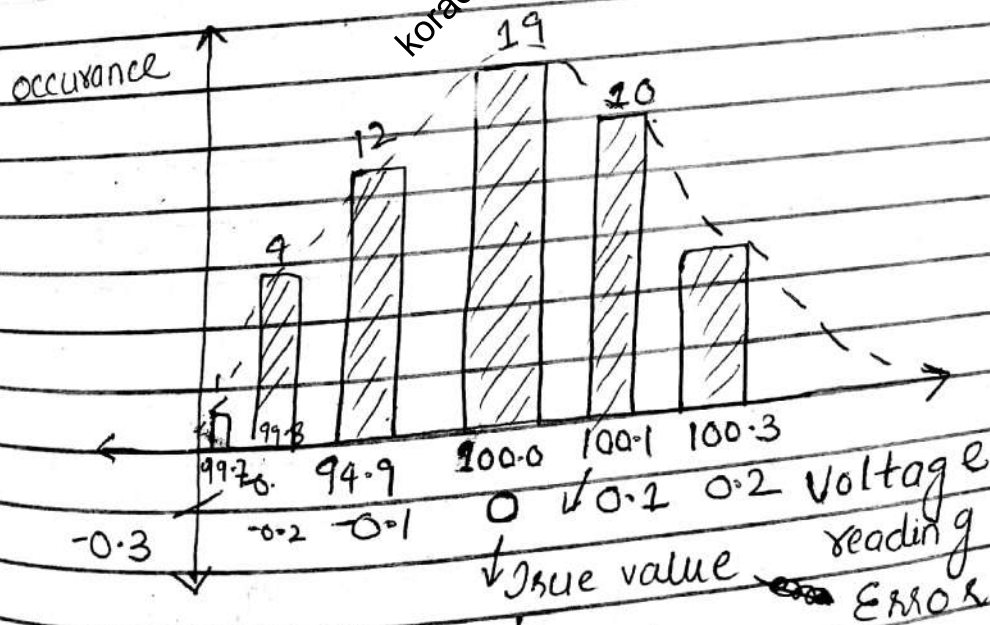
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Probability of Error :

Normal Distribution of Error :-

Voltage Reading (V)	Number of Readings
99.7	1
99.8	4
99.9	12
100.0	19
100.1	10
100.2	3
100.3	1

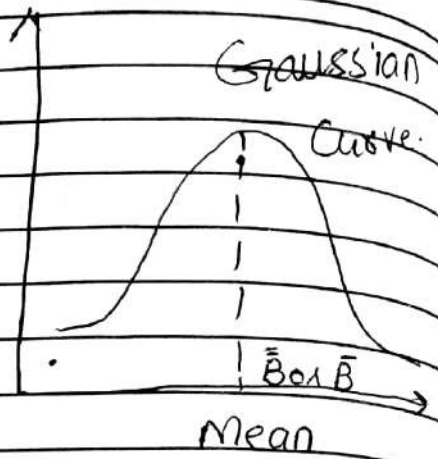


Bar Graph

As it has spaces

When no spaces then called Histogram.

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1) All observations include small disturbing effect called random errors

2) Random Error can be +ve or -ve.

3) There is an equal probability of +ve and -ve

### Error Distributions:

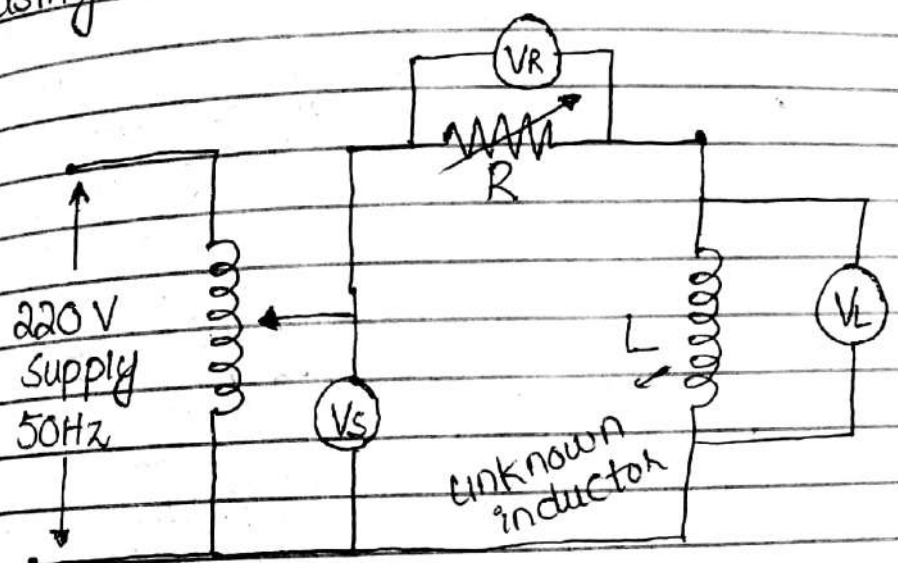
i) Small errors are more probable than large errors

ii) Large errors are ~~or~~ very im-probable (probability is less)

iii) There is an equal probability of +ve & -ve errors so that the probability of given error will be symmetrical about zero value.

# Experiment # 02 :-

To measure unknown inductance using three voltmeter method.



Auto transformer has only one winding

In transformer frequency will not change. In transformer there will be phase shift of  $180^\circ$  (at output)

$$E = -N \frac{d\phi}{dt}$$

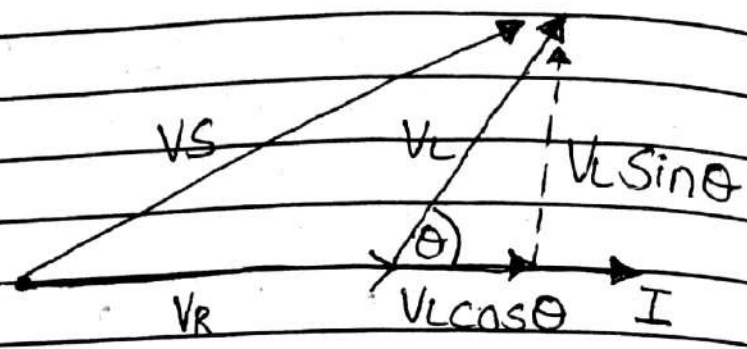
The resistance of rheostat changes by

$$R = \frac{S L}{A} \Rightarrow \boxed{R \propto L}$$

$$\boxed{V_S = V_R + V_L} \rightarrow \text{phasor sum}$$

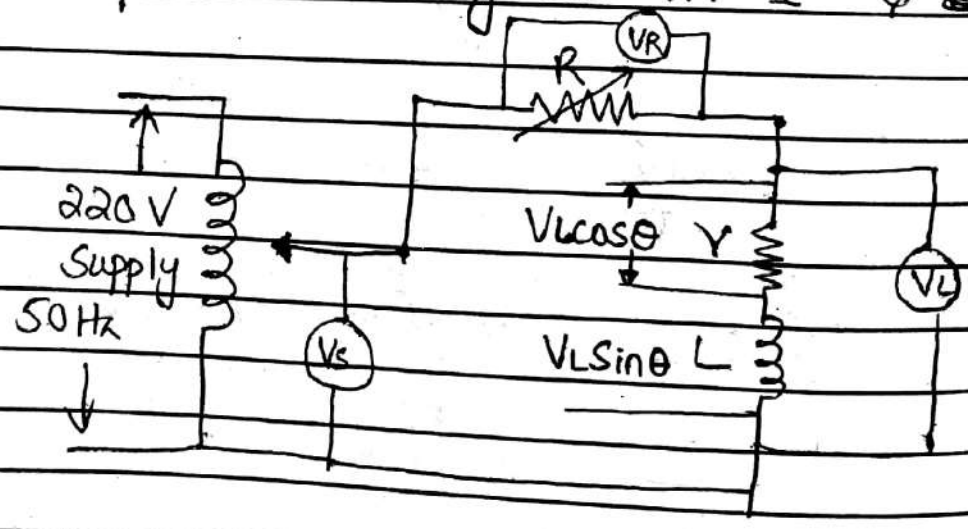
Its magnitude will be

$$\boxed{V_S = \sqrt{V_R^2 + V_L^2}}$$



There will be some resistance of inductor so  $V_L$  will lead behind the current by an angle of  $\theta$ . In ideal case when we consider zero resistance of inductor so  $V_L$  will lead behind current by an angle of  $90^\circ$ .

Impedance only lie in 1st & ~~3rd~~ <sup>4th</sup> Quad



% Relative Static Error:-

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Inst A	Inst B
Error = 1A	10A

We cannot say which instrument is more accurate.  
We can say which instrument is more accurate if we know relative static error.

$$\%RSE = \frac{\text{Error} \times 100}{\text{True}}$$

So true value is requisite to calculate %RSE.

A	B
True = 2A	True = 1000A

$$\%RSE = \frac{1}{2} \times 100 = 50\%$$

$$\%RSE = \frac{10}{1000} \times 100 = 1\%$$

Instrument B is more accurate.

$$V_L \sin \theta = I \times L$$
$$V_L \sin \theta = \frac{V_R}{R} \times 2\pi f L$$

$$L = \frac{V_L \sin \theta \cdot R}{2\pi f V_R}$$

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# LAB #03:- To learn some useful ftns of calculator

Shift + 7

→ Then press number (no)

1 Constants

2) Table generation:-

3) Unit conversion:-

↳ Shift + 8

$$101^{\circ} = 38.3^{\circ}C$$

Table generation:-

$$f(x) = e^x + 2^x + 3x^2 + 5$$

$$x = 1 - 9$$

x	f(x)
1	12.718
2	28.389
3	
4	
5	
6	
7	
8	
9	



for  $x \rightarrow \alpha + x \Rightarrow x$

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mode  $\rightarrow 7 \rightarrow$

Start =  $\frac{1}{9}$

End

Step size 1

$\rightarrow$  Equation solving :-

$$2x + 5y = 3$$

$$9x - 2y = -5$$

$$x = -0.387$$

$$y = 0.755$$

Mode  $\rightarrow$  Eqn(5)

Quadratic Eqn:

Alpha Calc

Mode 1  $2 \sqrt{x} = 1.2$

Mode 1

$$x = ?$$

$\rightarrow$  Shift + Calc } solve command

Solve for  $x$

0 and equal

$$x = -2.9266$$

$$e^{\frac{-x}{1-x^2}} = 0.8$$

$$x = ?$$

$$x = 0.070$$

Newton Raphson give on solution

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& that solution to

which our initial guess is  
near.

COMPLEX (Shift + 2)

$$2 \angle -45^\circ = \sqrt{2} + \sqrt{2}i$$

Shift (-)

Shift + 4 to

MATRIX:

add data

in B

$$A = \begin{bmatrix} 2 & 3 \\ 2 & 5 \end{bmatrix}, B = \begin{bmatrix} 1 & 2 \\ 2 & 3 \end{bmatrix}$$

$$A+B =$$

$$A \times B =$$

$$A^{-1} =$$

BASE - N

$$(295)_{10} = (127)_{16}$$

Mode 4 → Dec 295.

STAT: (Statistics)

Just we have to Enter data.

2, 3, 2, 5, 5, 4, 4.5, 2, 1, 3

Mode - 3

1 - 1 - var

Then type number

All clear (AC)

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Sum  
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Variance - 4  
 $n \rightarrow$  no of entries  
 $\bar{x} \rightarrow$  mean

$$\sum x =$$

$$S.D \left[ \begin{array}{l} \frac{\sum x^2}{n} \text{ (population)} \\ \frac{\sum x^2}{n-1} \text{ (sample)} \end{array} \right] = \begin{array}{l} 1.34257 \\ 1.415915 \end{array}$$

$x$	$f(x)$
2	50
3	30
4.5	22
5	10
3.5	5

Shift  $\rightarrow$  mode  $\rightarrow$  State  $\rightarrow$  fix ON

$$\bar{x} = 3.047$$

$$S_n = 1.0958$$

$$S_{n-1} = 1.1005$$

We can find Eqn of line using calculator.

If more than two points than calculator find Best fit line.

Mode  $\rightarrow$  Stat

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$$(x, y) = (2, 5), (3, 7)$$

$$Y = A + Bx$$

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$$Y = 1 + 2x$$

$$R = 1$$

$R = 1$  mean best fit

~~Q~~ CURVE.

$$Y = ?$$

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One meter is the length of path traveled by light in vacuum in time interval of  $\frac{1}{299,792,458}$  sec.

299,792,458

2 hundred 99 million 7 hundred & 92 thousand 4 hundred & fifty eight.

Kilogram:

One kg of mass is the mass of ~~intext~~ international prototype of kg (platinum, Iridium cylinder) kept at International Bureau of weights and measure near Paris.

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One Second

SECOND:-  
One second is duration of

9,192,631,770

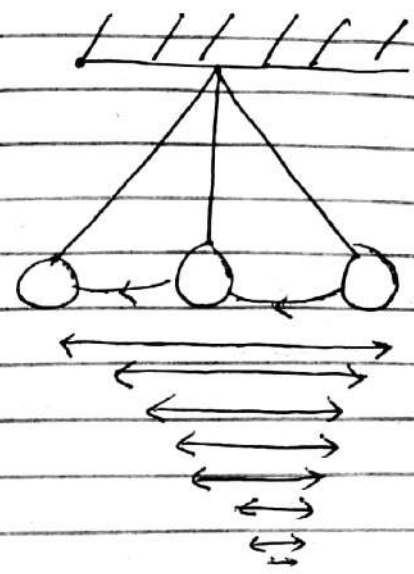
periods of radiations corresponding to transition between two hyperfine levels of ground state of Cs-133 atom.

Cesium clocks are the most accurate watches and clocks.

This definition was define in 1967.

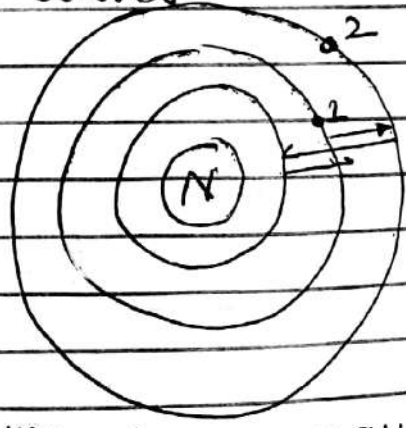
-273.15°C is that temperature at which all the molecular motions in water is are ceased. and this is equal to zero kelvin.

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Time period will remain same in each case because according speed will reduce.

Cesium will release energy in the form of Electromagnetic waves



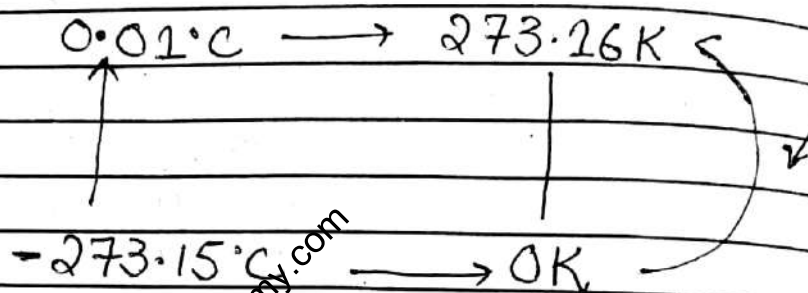
we give energy to the electron of cesium atom & it vibrate about mean position

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$0.01^{\circ}\text{C}$  is called as triple point

At this stage all three states of water exist

One Kelvin is deflection of thermodynamic temperature of triple point of water.



Mole:

One mole is the amount of substance which contains as many elementary particles as in  $0.012\text{kg}$  of carbon.

Candela:

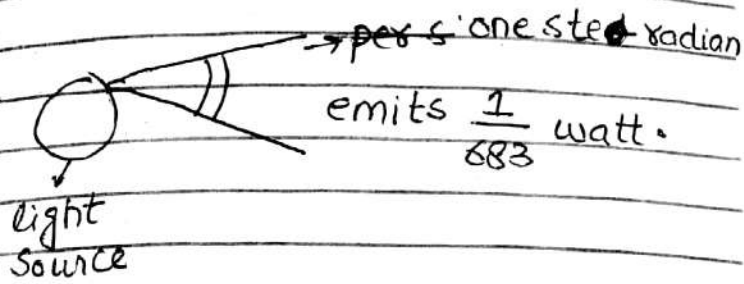
One candela is a luminous intensity of the source that emits monochromatic radiation of frequency

$540 \times 10^{12}\text{Hz}$ , and that has radiant intensity in that direction of  $1$  watt  $683$

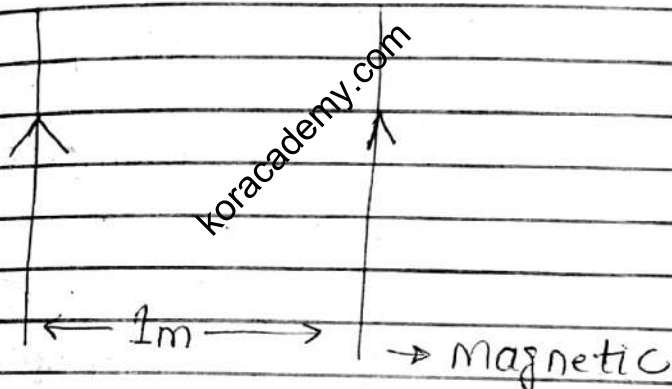
$540 \times 10^{14} \text{ Hz} \rightarrow$  freq of red light

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per steradian angle.



Ampere is the unit of electric current



If current flows in same direction they will attract  
Each wire each other

Force b/w them is  $2 \times 10^{-7} \text{ N/m}$

Distance is 1m.

So the current is 1A



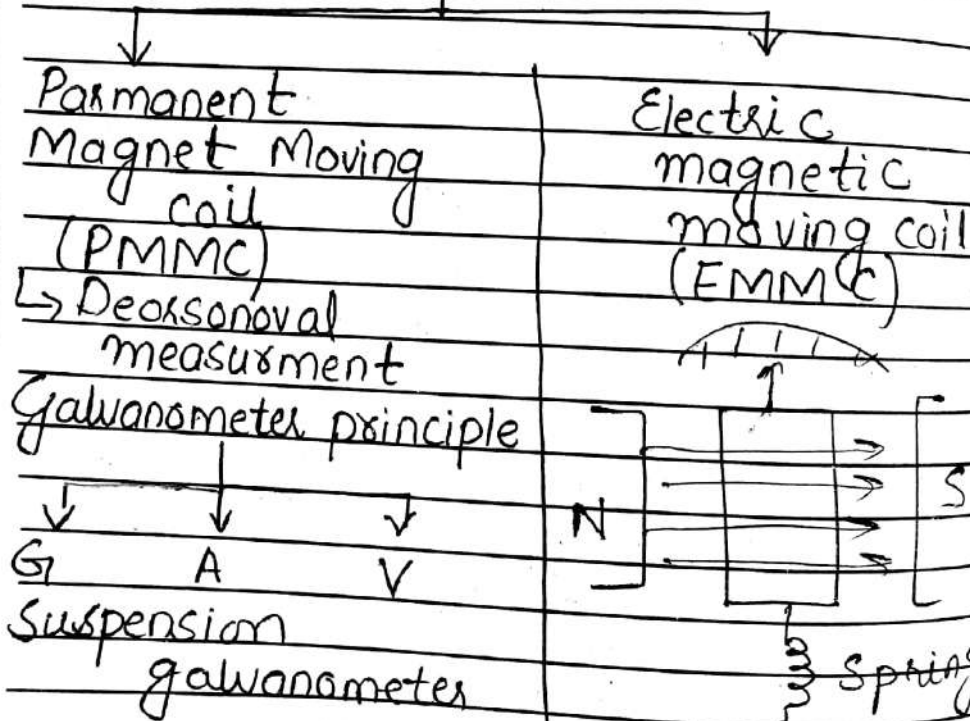
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1A is that constant current which will be maintained in two straight parallel conductors of infinite length, negligible cross-section and negligible place one meter apart in vacuum would produce b/w them a force of  $2 \times 10^{-7} \text{ N/m}$  length

## LECTURE NO 04

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### Moving coil Instruments



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Two types of torques:

- 1) Deflection torque
- 2) Opposing torque (due to spring)

Torque & Deflection of galvanometer: -

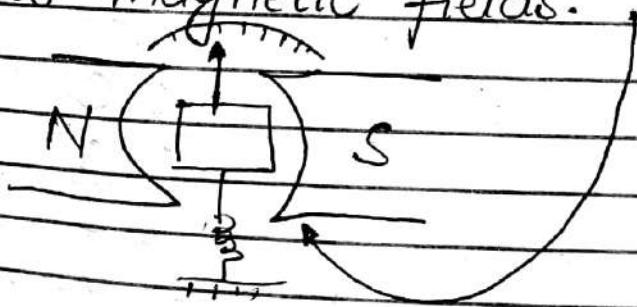
Steady State Deflection: -

The equation for the developed torque, derived from the basic law for electromagnetic torque.

$$T = B \times A \times I \times N$$

$$T = BINA \sin \theta \rightarrow \text{Angle b/w } \vec{B} \text{ \& } \vec{I}$$

We can to maximize the interaction of two magnetic fields.



We use concept of Radial magnetic field to maximize torque and make the angle b/w the A vector and the B 90 degree

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i-e making cylindrical magnet and cylindrical soft iron coil.

We use soft iron because it magnetizes easily.

Applied Torque = Restoring torque

or

$$NAIB = C\phi \quad \text{for which} \quad I \propto \phi$$

where  $C$  is torsional constant and is proportional to the angle of twist in spring  $\phi$  (which is angle of twist in degree)

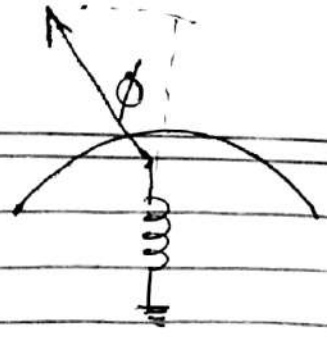
$\phi$ (deg)	$C$
1	$1C$
2	$2C$
3	$3C$

$C \rightarrow$  Depends on nature of spring.

Date:   /  /  

$$I \propto \phi$$

It depends on  $B, N, A$  and  $C$



Sensitivity of Galvanometer:-

$$\text{Current sensitivity} = \frac{\phi}{I}$$

= Deflection in Pointer  
change in current

$$\text{So } NIAB = C\phi$$

which means 
$$\frac{\phi}{I} = \frac{NAB}{C}$$

When we use it as a voltmeter

Voltage Sensitivity  $\frac{\phi}{V}$  where  $V = IR$

$$V = \frac{C\phi}{NABR}$$

So 
$$\frac{\phi}{V} = \frac{NAB}{CR}$$

~~to~~  $R \rightarrow$  Resistance of high resistor connected in Series.

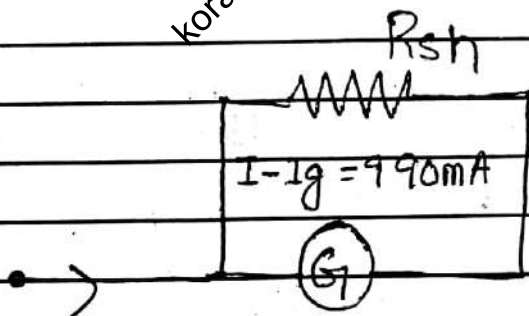
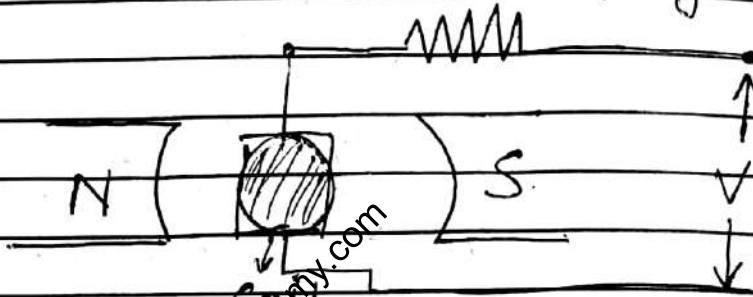
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## Dynamic Behaviour:

damping constant ( $D$ )  $\rightarrow$  affected by air/oil etc

Resistance of winding is less than  $1\Omega$

$R_{series}$  (High resistance)

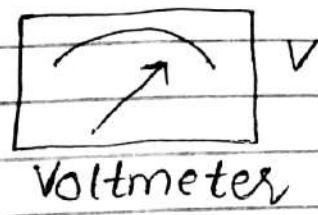


$$I_A = 1000\text{mA}$$

$$I_g = 10\text{mA}$$

Date: 11 Sir Jazooz

1) Indicating type Instrument  
Display

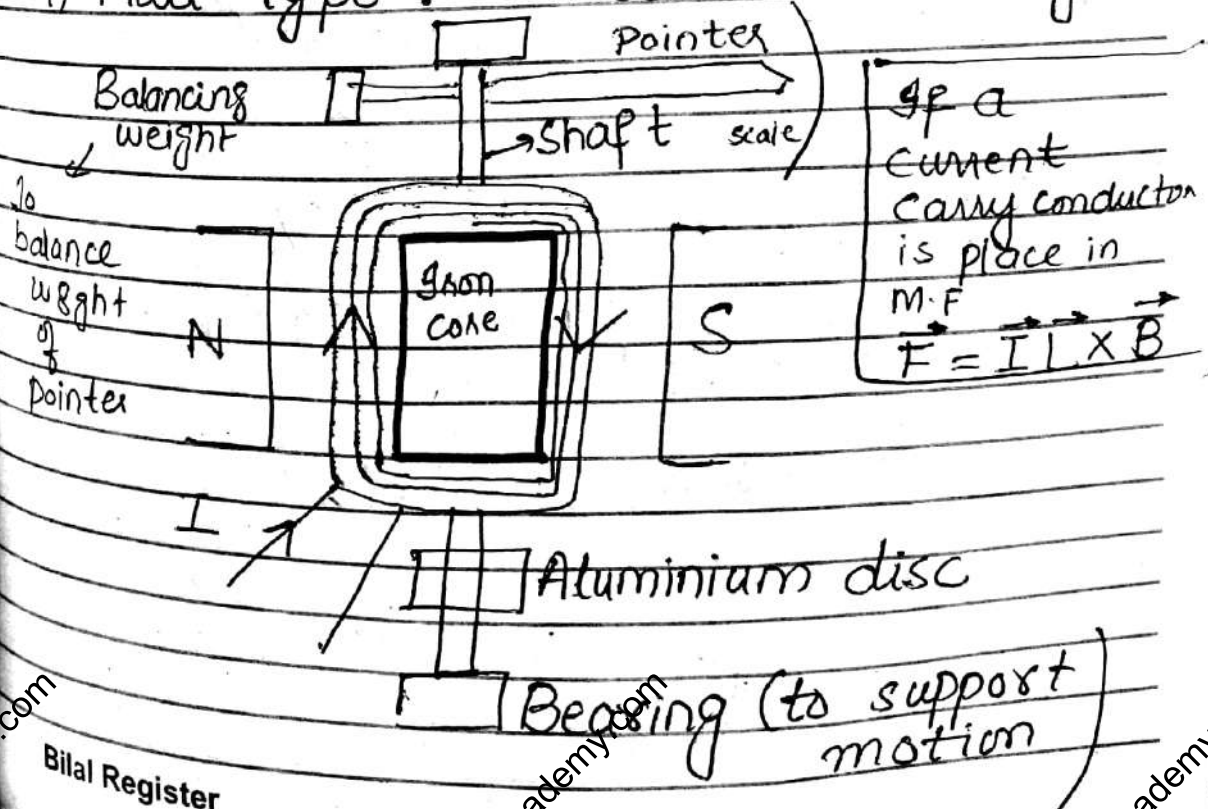


2) Recording type instrument  
Display + Recording

3) Integrating type instrument  
Display + Recording + commulative addition

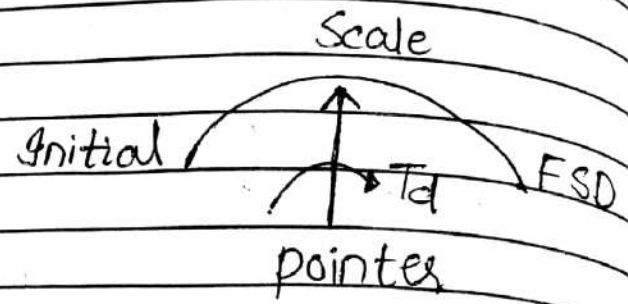
Eg: Energy meter. (964 → 965)

4) Null type : wheat stone bridge.



Date:   /  /  

Due to deflecting torque pointer start moving from initial point to full scale deflection.



$$T_d \propto I, \quad T_d \propto \phi, \quad T_d \propto N$$

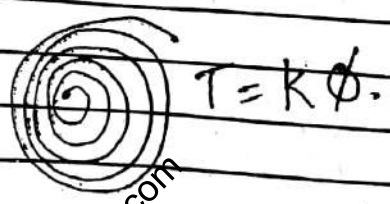
$$T_d \propto NI\phi$$

$$T_d = \frac{2}{\pi} ANI \Rightarrow \boxed{T_d \propto I}$$

As current is continuously there so torque will be also there. So stop pointer at certain scale we need second torque i.e.

## 2) Controlling Torque ( $T_c$ )

We use spiral spring for this purpose.



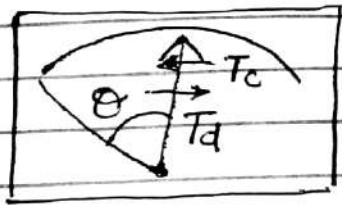
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The pointer will stop if both torques becomes equal.

$$T_c = K\theta$$

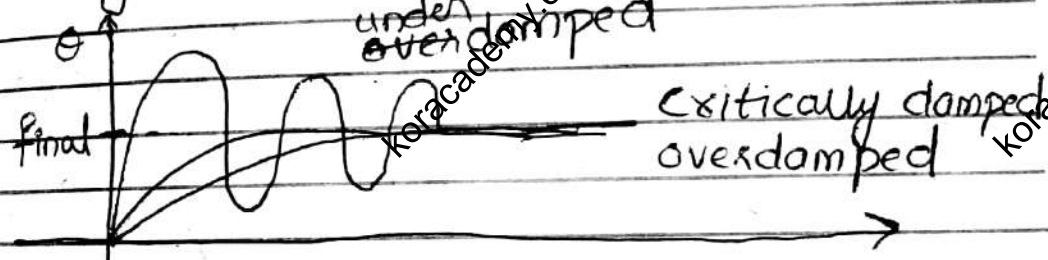
$$T_d = T_c$$

$$BAN I = K\theta$$
$$\theta = \frac{BAN I}{K}$$



$$\theta = CI \Rightarrow \theta \propto I$$

Scaling is uniform under overdamped



### ③ Damping Torque ( $T_{damp}$ )

→ Aluminium disc

↓  
Magnetic field linked due to vibration

↓  
According to Lenz's law opposite its cause

↓  
Eddy current will flow in Aluminium disc.

Bilal Register



Date:   /  /  

## Temperature Control: -

Two problems due to temperature

$$R_t = R_0 (1 + \alpha \Delta T)$$

$\alpha = +ve$  for metals

$R \propto T$

Metals have positive temperature co-efficient

$\uparrow T \Rightarrow \uparrow R_t$

Semi-conductor has -ve temperature co-efficient

$\uparrow T \Rightarrow \downarrow R_t$

$$R_t < R_0$$

$$\alpha = -ve$$

Manganin (Mn)  $\Rightarrow \alpha = 0$

No effect of temperature on resistance.

As coil is of copper

$\uparrow T \Rightarrow \uparrow R$

Value of current will reduce

Galvanometer will read low (due to temperature increase).

Bilal Register

Date:   /  /  

2) Due to  $T \uparrow$  softness of spring will increase.

Galvanometer will read high.

1st effect is more than 2nd one. Galvanometer will read low.

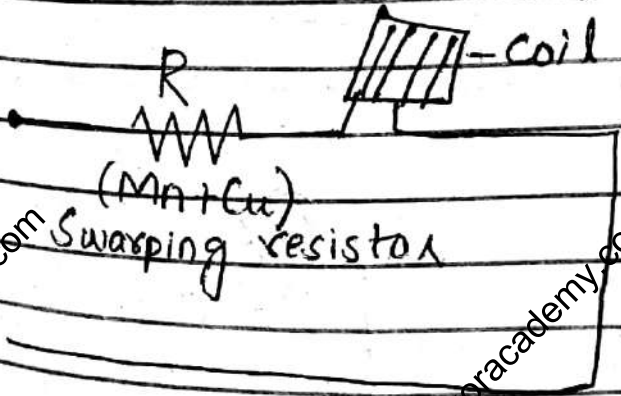
### Temperature Compensating:-

If two effects becomes equal.

To overcome the first effect we connect a resistor in series with the coil, made up of (Mn + Cu). The

resistor is called swamping resistor.

~~Q.20~~: Mn - Cu  
20 : 1 or 30 : 1



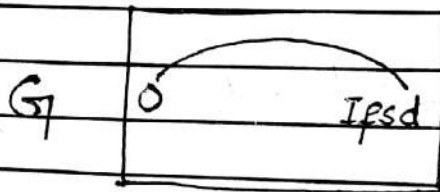
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# DC AMMETERS:

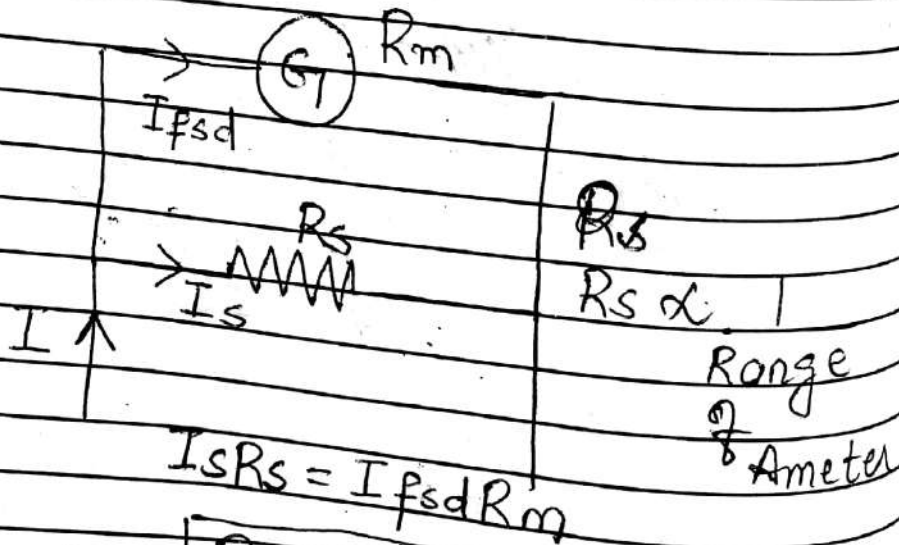
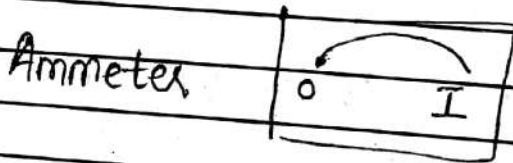
Galvanometer are use for sensing current.

Conversion of galvanometer to ammeter:-

Galvanometer 0 to  $I_{fsd}$



A) 0 to I



$$I_s R_s = I_{fsd} R_m$$

$$R_s = \frac{I_{fsd} R_m}{I - I_{fsd}}$$

Bilal Register

Date: 11

Example:

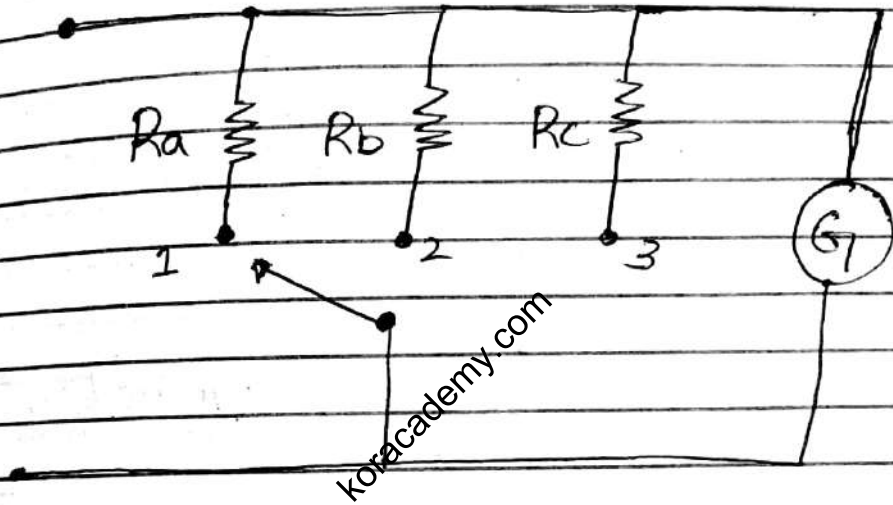
$$I_{fSD} = 1 \text{ mA}$$

$$R_m = 100 \Omega$$

$$I = 100 \text{ mA}$$

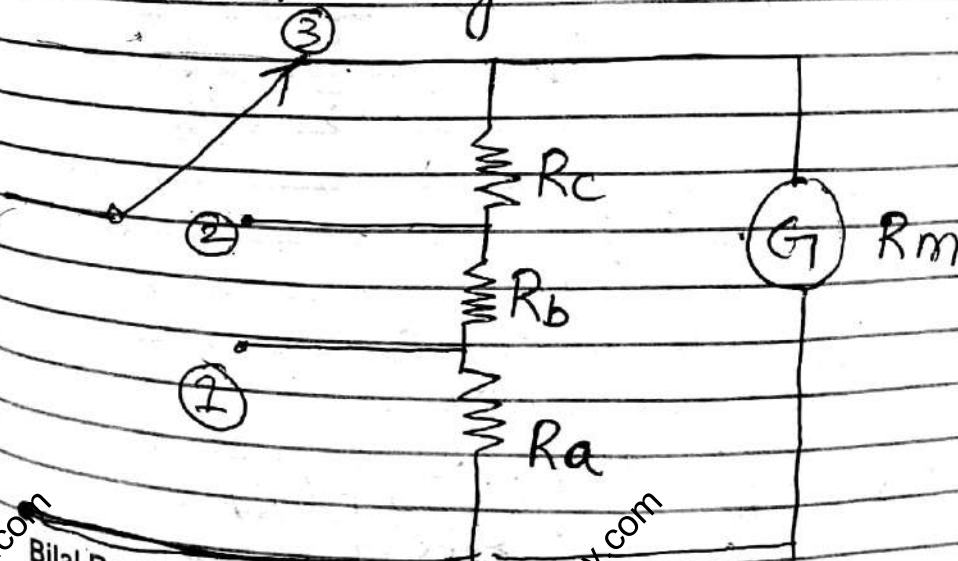
$$R_s = 1.01 \Omega$$

Multi-range Ammeter:



Limitation: If switch is in between 1 & 2 a lot of current can flow through galvanometer & it can damage galvanometer.

Universal or Ayrton shunt:



Bilal Register

Date:   /  /  

### Exple 4.2

We need three ranges

1A, 5A and 10A

Internal resistance of galvanometer  
is  $50\ \Omega$

$$I_{fsd} = 1\text{mA}$$

Find  $R_A$ ,  $R_B$  and  $R_C$ .

As  $R_s \propto I$

change of Ammeter

so At point 3:

$$I = 1\text{A}, R_m = 50\ \Omega$$

$$R_s = R_a + R_b + R_c$$

$$R_a + R_b + R_c = \frac{1 \times 50}{1000 - 1}$$

$$R_a + R_b + R_c = 0.05005 \quad \text{--- (a)}$$

At point 2:

$$I = 5\text{A}$$

$$R_m = 50 + R_c$$

$$R_s = R_a + R_b$$

$$R_a + R_b = \frac{1 \times (50 + R_c)}{5000 - 1}$$

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$$R_a + R_b - 0.00220004 R_c = 0.010002 \quad \text{--- (b)}$$

At point-3

$$I = 10A$$

$$R_m = 50 + R_b + R_c$$

$$R_s = R_a$$

$$R_a = \frac{1 \times (50 + R_b + R_c)}{10,000 - 1}$$

$$R_a = 0.00010001$$

$$R_a + R_b - 0.00020004 R_c = 0.010002$$

$$R_a - 0.00010001 R_b - 0.00010001 R_c = 0.0050005$$

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Oct 22; 2019

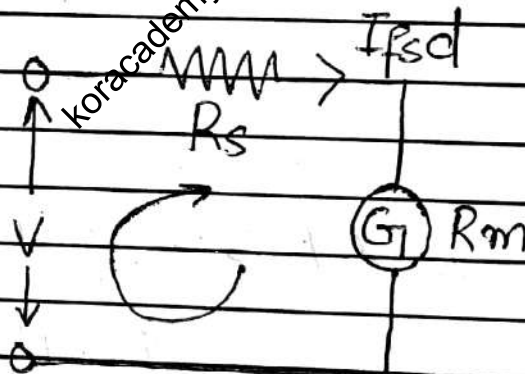
# LECTURE #

## DC VOLTMETER:

(G) 0 to  $I_{fsd}$

(V) 0 to V volts

Conversion of galvanometer to voltmeter



voltmeter

If we apply  $V$  volts then Galvanometer has to give full scale deflection &  $G$  give full scale deflection if  $I_{fsd}$  current pass through it

Applying KVL

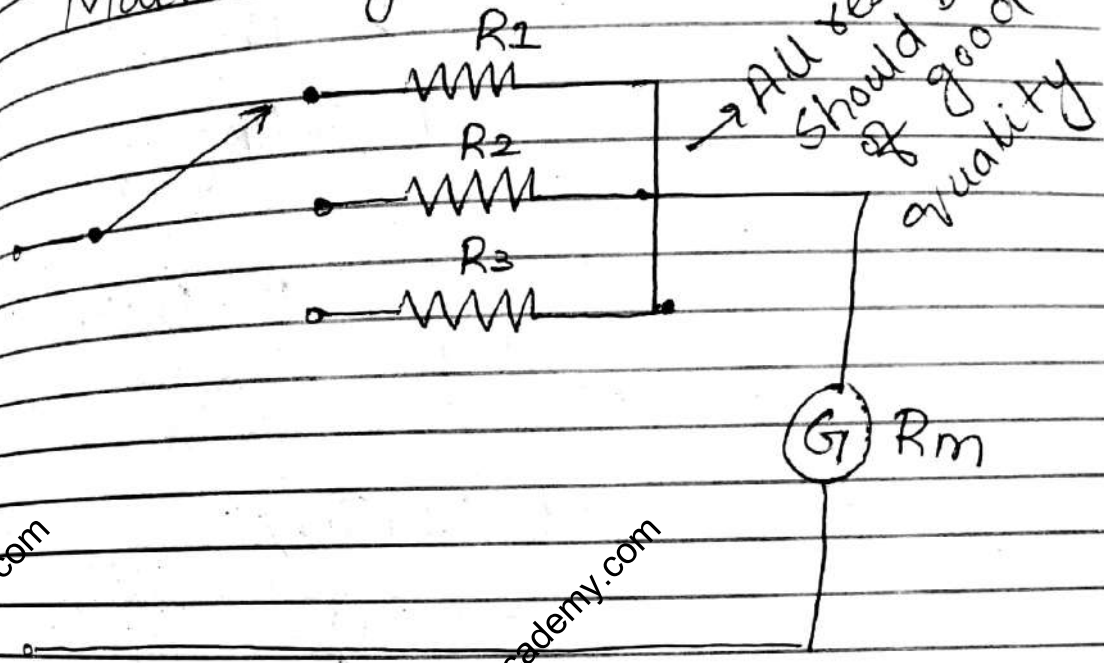
$$V = I_{fsd}(R_m + R_s)$$

$$\frac{V}{I_{fsd}} = R_m + R_s$$

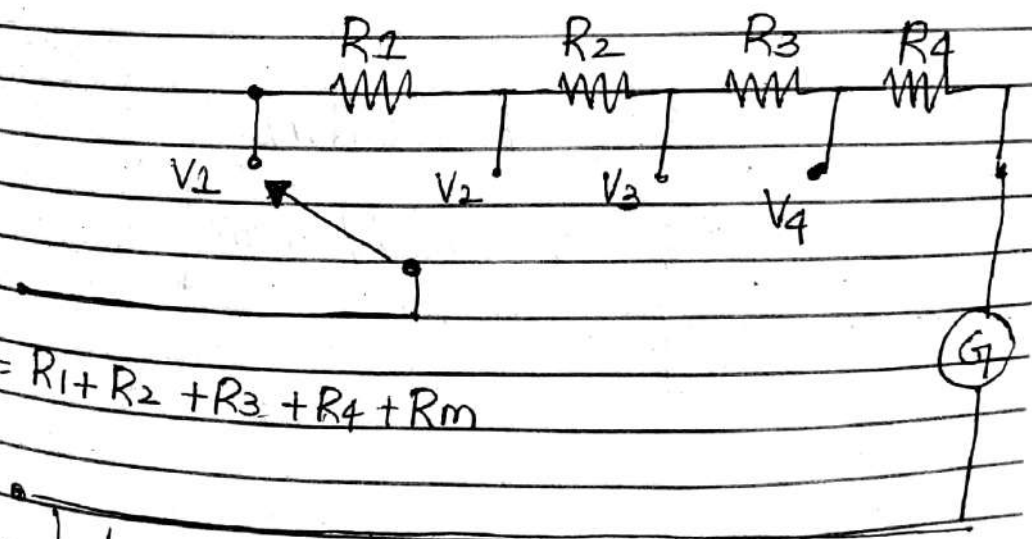
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$$R_s = \frac{V}{I_{fsd}} - R_m$$

### Multi-Range Voltmeter



### More practical solution



↓  
R4 should be standard & of high quality.

→ less Expensive



Date:   /  /  

Exple 4.3:

Voltmeter Sensitivity:-

It is define as

"e Ohms per volt rating of  
voltmeter."

$$S = \frac{R_T}{V_{fsd}}$$

$$R_T = R_s + R_m$$

$$V_{fsd} = I_{fsd} (R_s + R_m)$$

$$V_{fsd} = I_{fsd} (R_T)$$

$$S = \frac{R_T}{V_{fsd}} = \frac{1}{I_{fsd}}$$

$$S \times V = R_s + R_m$$

$$R_s = (S \times V) - R_m$$

Exple 4.4

Date:   /  /  

# LOADING EFFECT:-

Current carrying capacity load is known as load.

Load  $\uparrow$  I  $\uparrow$  P  $\uparrow$  R  $\downarrow$

Higher load means low resistance.

Voltmeter has loading effect because

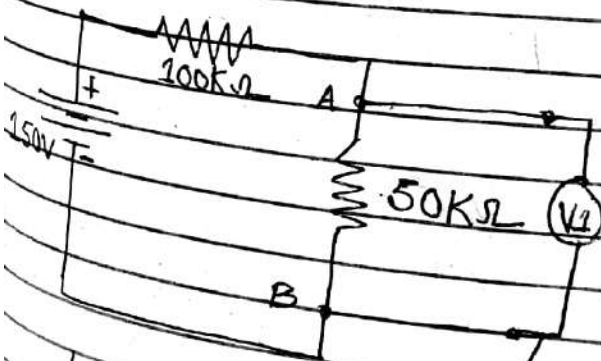
we connect voltmeters in parallel the equivalent resistance will

decrease, the load will increase, ckt will draw more

then

current.

## Example 4.5:-



Loading Register Effect

Resistance will now decrease b/w A & B

If two fans are connected in parallel the equivalent resistance will decrease

100W R  $\uparrow$   
200W R  $\downarrow$

W 100W

W 200W

In parallel 200W will glow more

$$P = \frac{V^2}{R} \quad V = \text{const}$$

In series 100W will glow more

$$P = I^2 R$$

$$I = \text{const}$$

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$V_1$  has full scale deflection = 50V

$V_2$  " " " " = 50V

$$V_1 \rightarrow S_1 = \frac{1000 \Omega}{V}$$

$$V_2 \rightarrow S_2 = \frac{20,000 \Omega}{V}$$

$$V_T = \frac{50K\Omega \times 150}{100K + 50K}$$

$$V_T = 50 \text{ volts}$$

If we connect voltmeter no 1:-  
 $R_1 = S_1 \times V_{fsd}$

$$R_1 = 1000 \times 50$$

$$R_1 = 50K\Omega$$

$$R_{AB} = 50K // 50K$$

$$R_{AB} = 25K\Omega$$

$$V_1 = \frac{150 \times 25}{100 + 25}$$

$$V_1 = 30V$$

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$$\text{Percentage } \epsilon_{\text{MOR}} = \frac{50 - 30}{50} \times 100$$

$$= \frac{20}{50} \times 100$$

= 40%. Due to loading effect.

If we connect Voltmeter no 2

$$R_2 = S_2 \times V_{\text{fsd}}$$

$$= 20,000 \times 50$$

$$R_2 = 1,000,000$$

$$R_2 = 1 \text{ M}\Omega$$

In ammeter no loading effect

$$R_{AB} = 1 \text{ M}\Omega // 50 \text{ K}\Omega$$

$$R_{AB} = 47.6 \text{ K}\Omega$$

$$V_2 = \frac{150 \times 47.6}{100 + 47.6}$$

$$V_2 = 48.36 \text{ V}$$

$$\text{Percentage } \epsilon_{\text{MOR}} = \frac{50 - 48.36}{50} \times 100$$

$$= 3.28\%$$

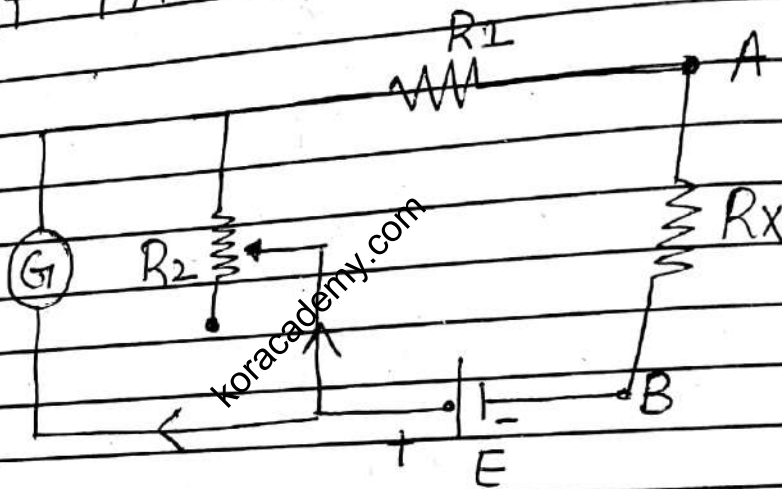
the  $\epsilon_{\text{MOR}}$  has reduce significantly

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If ckt contains lower resistances so then use  $V_1$

If ckt contains higher resistance so then use  $V_2$ .

→ SERIES TYPE OHMMETER :-  
→ SHUNT TYPE OHMM



It can be made from galvanometer  
 $E \rightarrow$  voltage of internal battery

$R_m \rightarrow$  Internal resistance of galvanometer

$R_1 \rightarrow$  Current limiting resistor

$R_2 \rightarrow$  zero adjust resistor.

$R_x \rightarrow$  unknown resistor b/w point  
A & B.

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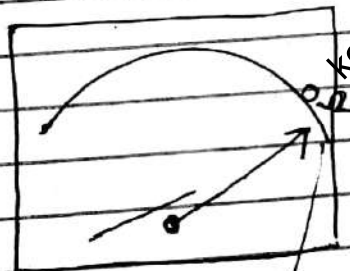
We need to calibrate the  
ga galvanometer in terms  
of ohms. (to measure  
resistance of  $R_x$ )

CASES:-

1)  $R_x = 0 \Omega$  (Battery will provide  
maximum current)

Adjust  $R_2$  such that the  
galvanometer give full scale  
deflection. ( $I_{fsd}$ )

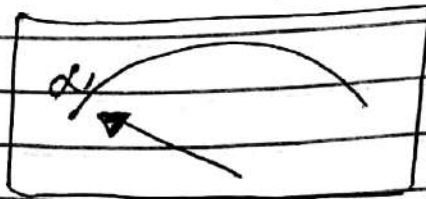
Means we will increase  $R_2$   
till galvanometer give full scale  
deflection.



2)  $R_x = \infty$

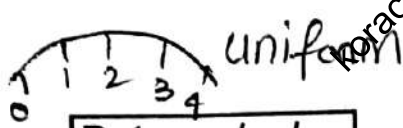
From Pt A & B  
remove  $R_x$

Galvanometer will give  
zero deflection  
as ckt is open.



Scale will be non-uniform.

Linear (uniform)



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The scale will be non uniform.

To calibrate the middle points there are different methods.

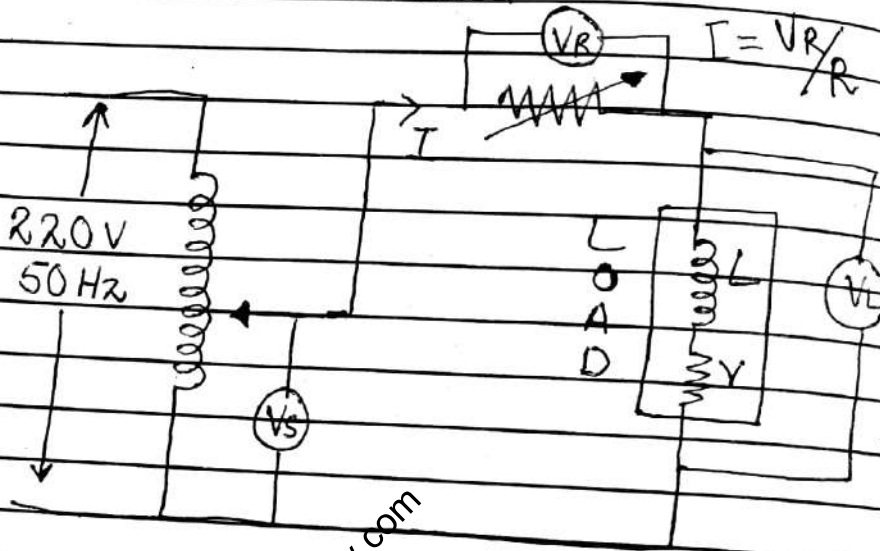
Take standard resistor whose  $R$  is known and see deflection of galvanometer & calibrate scale accordingly. (connecting them one by one)

Whenever we use series type ohm meter then first of all short A and B & adjust  $R_2$  to give so that galvanometer give full scale deflection. (Because battery voltage will reduce w.r.t time)

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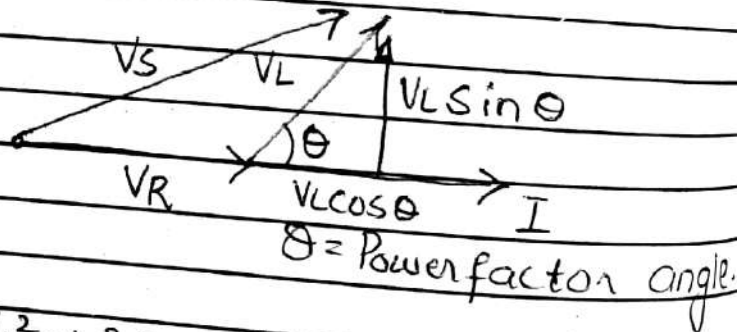
LAB #04:-

To measure the single phase power using three voltmeter method.



$$V_s = V_R + V_L$$

$$P \text{ of } = \frac{P}{S}$$



$$V_s^2 = V_L^2 \sin^2 \theta + (V_R + V_L \cos \theta)^2$$

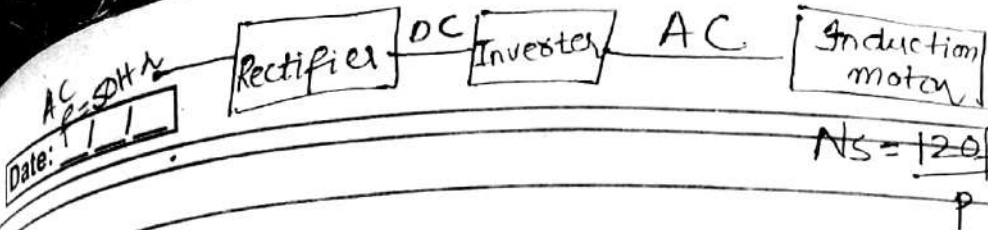
$$V_s^2 = V_L^2 \sin^2 \theta + V_R^2 + V_L^2 \cos^2 \theta + 2V_R V_L \cos \theta$$

$$V_s^2 = V_L^2 (\sin^2 \theta + \cos^2 \theta) + V_R^2 + 2V_R V_L \cos \theta$$

$$V_s^2 - V_L^2 - V_R^2 = 2V_R V_L \cos \theta$$

Bilal Register





$$\cos\theta = \frac{V_s^2 - V_L^2 - V_R^2}{2V_R V_L} \quad \left. \vphantom{\cos\theta} \right\} \text{Power factor of the load}$$

$$P = V_L I \cos\theta$$

$$P = \cancel{V_L} \left( \frac{V_R}{R} \right) \left[ \frac{V_s^2 - V_L^2 - V_R^2}{2V_R \cancel{V_L}} \right]$$

$$P = \frac{V_s^2 - V_L^2 - V_R^2}{2R}$$

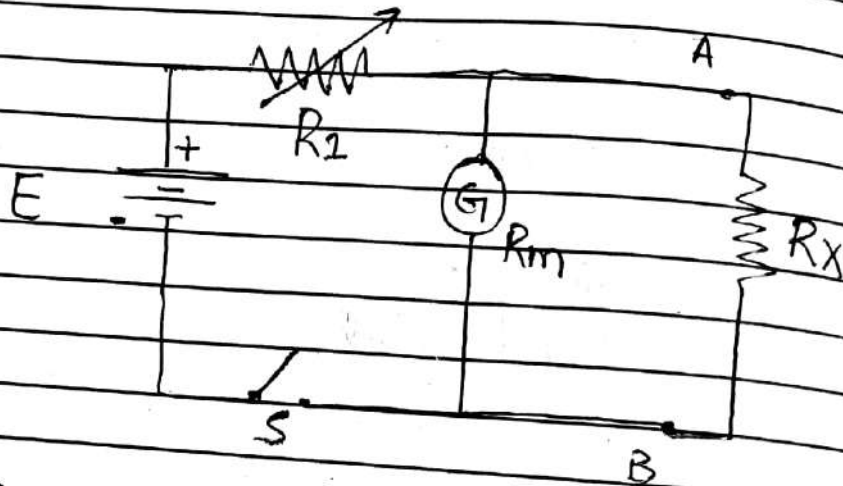
S.No	V <sub>s</sub>	V <sub>R</sub>	V <sub>L</sub>	R	P
1	20.9	16.5	4.2	200 Ω	
	30	23.72	5.7		
	40	32.85	7.74		
	50.54	40.69	9.39		

$$P = 750 \text{ watt}$$

Date:   /  /  

# LECTURE

## SHUNT TYPE OHMMETER:



$R_2 \Rightarrow$  Current limiting resistor

$R_m \Rightarrow$  Internal resistance of ammeter

$R_x \Rightarrow$  unknown resistance

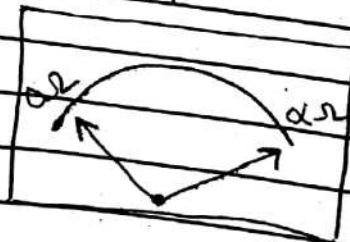
Cases:

1)  $R_x = 0 \Omega$  (short circuit)



No Deflection

$R_x = 0 \Omega$

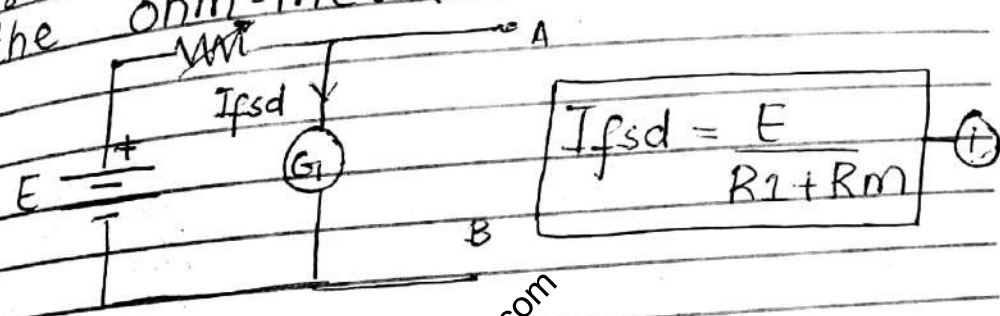


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$R_x = \alpha \Omega$  (open ckt)

2) we will adjust  $R_1(\downarrow)$  such that galvanometer gives full scale deflection.

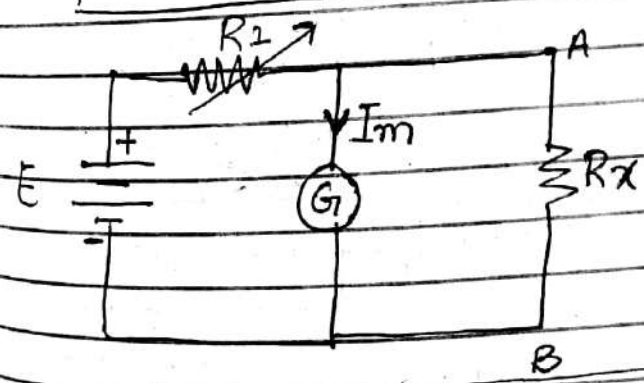
Then we will take known resistances and calibrate the ohm-meter



$$I_{fsd} = \frac{E}{R_1 + R_m}$$

$$R_1 = \frac{E}{I_{fsd}} - R_m$$

(2)



$$I = \frac{E}{R_2 + R_m \parallel R_x}$$

(3)

$$I_m = I \times \frac{R_x}{R_m + R_x}$$

$$I_m = \frac{E}{R_2 + R_m} \times \frac{R_x}{R_m + R_x}$$

$$I_m = \frac{E R_x}{R_2 R_m + R_2 R_x + R_m R_x} \quad \text{--- (4)}$$

Dividing eq (4) by eq (1)

$$\frac{I_m}{I_{fsd}} = \frac{E R_x}{R_2 R_m + R_2 R_x + R_m R_x} \times \frac{R_2 + R_m}{E}$$

$$\frac{I_m}{I_{fsd}} = \frac{R_x (R_2 + R_m)}{R_x (R_2 + R_m) + R_2 R_m}$$

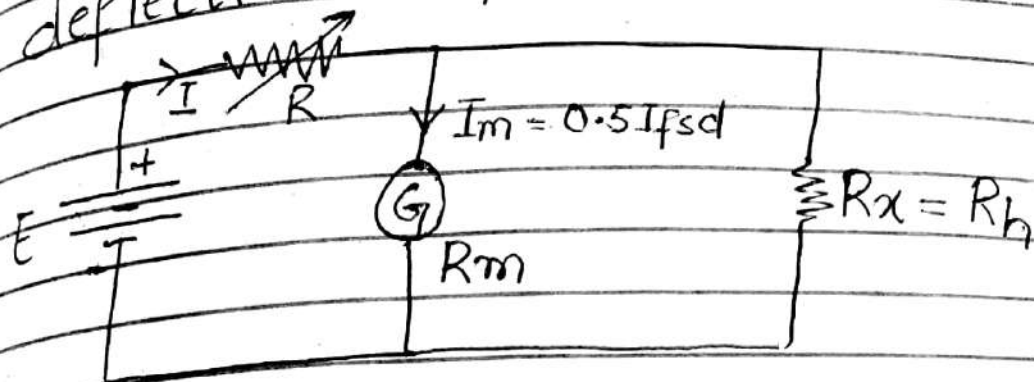
$$\frac{I_m}{I_{fsd}} = \frac{R_x}{R_x + \frac{R_2 R_m}{R_2 + R_m}}$$

$$\boxed{\frac{I_m}{I_{fsd}} = \frac{R_x}{R_x + R_p}} \quad \text{--- (5)}$$

The scale will be non uniform as relation b/w  $I_m$  &  $R_x$  is non linear.

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We can differentiate two ohm-meter by half scale deflection point.



$$R_x = R_h$$

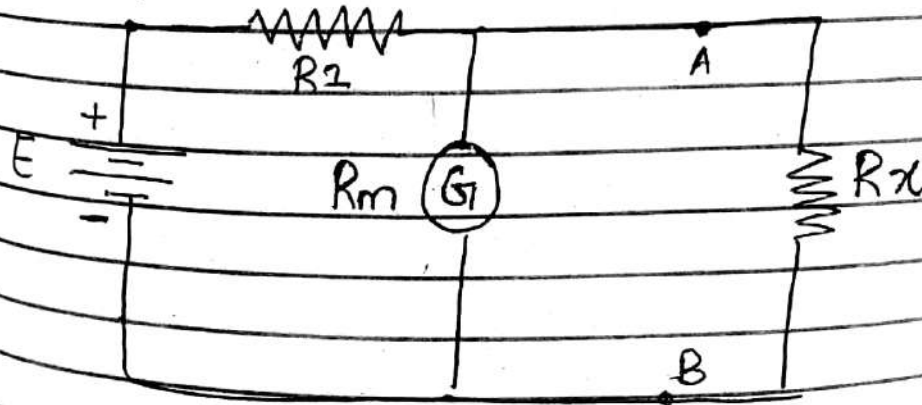
$$I_m = 0.5 I_{f.s.d}$$

$$\frac{0.5 I_{f.s.d}}{I_{f.s.d}} = \frac{R_h}{R_m + R_p}$$

$$R_h = R_p = \frac{R_m R_2}{R_m + R_2}$$

$R_h$  is Equal to internal resistance of galvanometer

### Example 4.8 (Imp)



$$I_{f.s.d} = 10 \text{ mA}$$

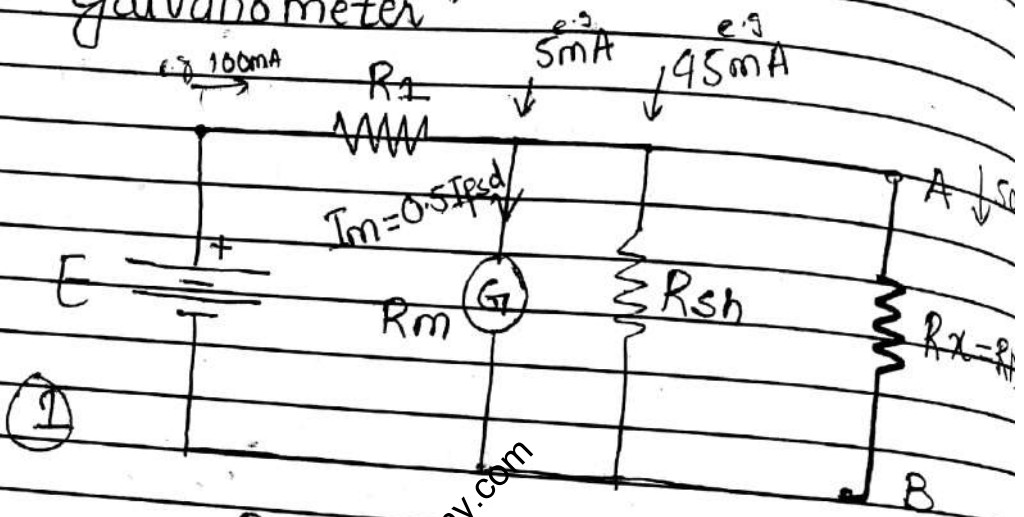
$$R_m = 5 \Omega$$

$$E = 3 \text{ V}$$

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$R_1 > R_m$

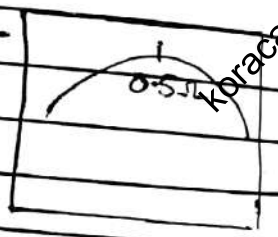
Q) want to modify ckt by connecting shunt by resistance parallel to Galvanometer



$R_h = 0.5 \Omega$

Find

- a)  $R_{sh} = ?$
- b)  $R_1 = ?$



a)  $R_{sh} = ?$

$R_x = R_h$

$I_m = 0.5 I_{fsd}$   
 $= 0.5 \times 10$

$I_m = 5 \text{mA}$

$E_m = I_m R_m$

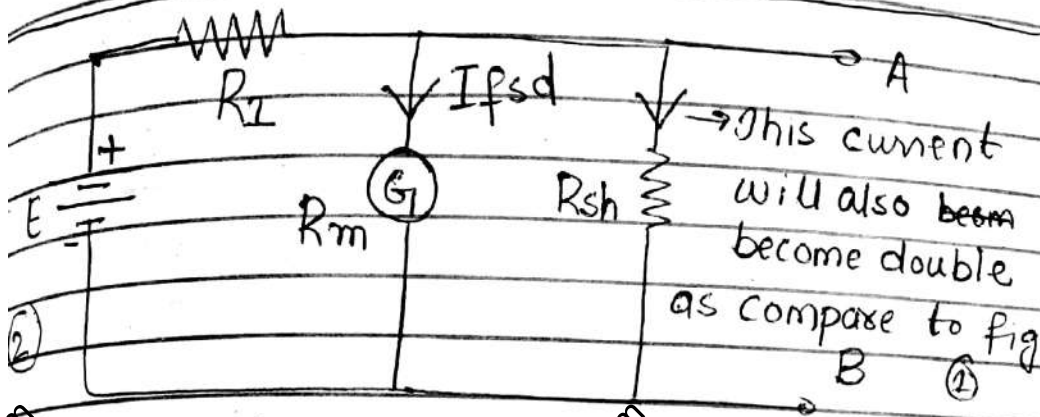
$= 5 \times 5$

$E = 25 \text{mV}$

Bilal Register

$$I_x = \frac{E_m}{R_n} = \frac{25}{0.5}$$

$$I_x = 50 \text{ mA}$$



Current will be same in (1) & (2) (almost constant)

Battery is providing almost same current.

In fig (1) due to  $R_n$  the meter current become half.

100mA	10mA	90mA	e.g
-------	------	------	-----

$$I_x = I_m + I_{sh}$$

$$I_{sh} = I_x - I_m$$

$$I_{sh} = 50 - 5$$

$$I_{sh} = 45 \text{ mA}$$

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$$R_{sh} = \frac{E_m}{I_{sh}} = \frac{25}{45}$$

$$R_{sh} = \frac{5 \Omega}{9}$$

Part B)

Find  $R_2$ ?

$$I = I_m + I_{sh} + I_x$$

$$I = 5 + 45 + 50$$

$$I = 100 \text{ mA}$$

$$E = E_1 + E_m$$

$$E_1 = E - E_m$$

$$= 3 - 25 \times 10^{-3}$$

$$E_1 = 2.975 \text{ V}$$

$$E_1 = IR_2$$

$$R_2 = \frac{E_1}{I} = \frac{2.975}{100 \times 10^{-3}}$$

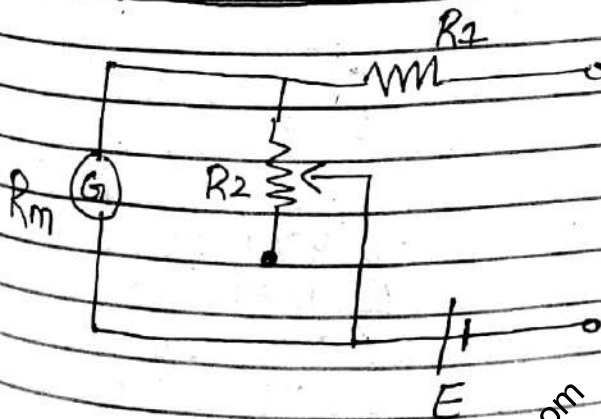
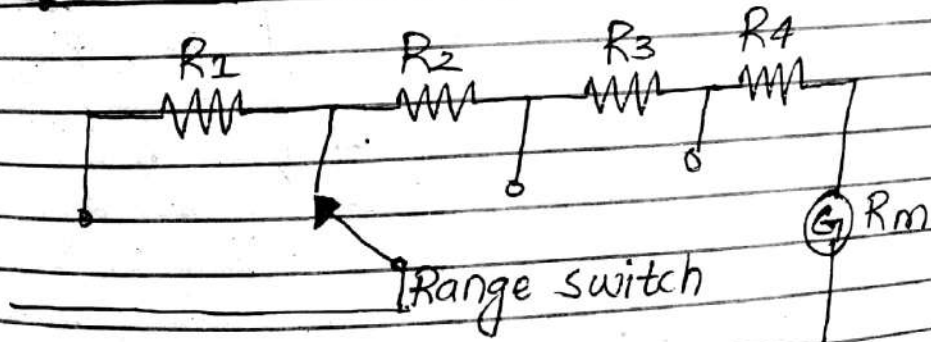
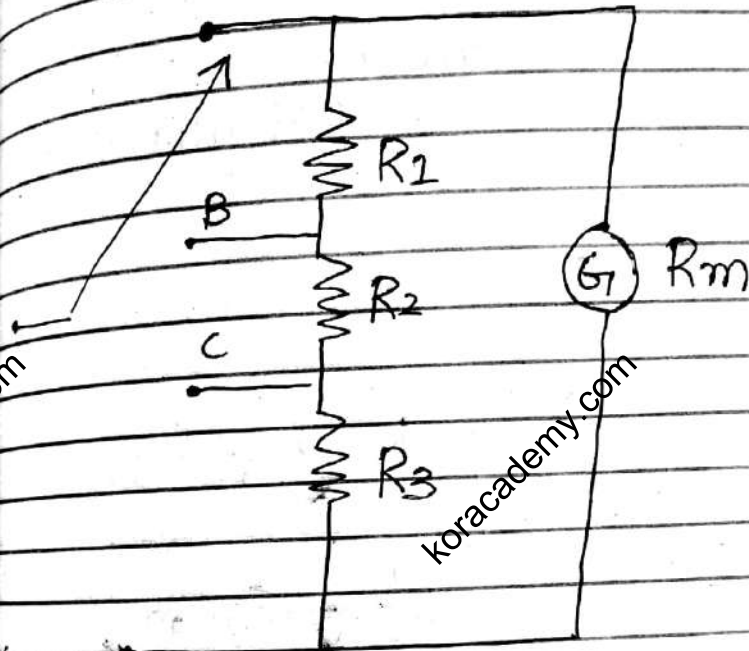
$$R_2 = 29.75 \Omega$$



Date:   /  /  

# Multimeter or VOM:

VOM (volt, ohm, milliamp)



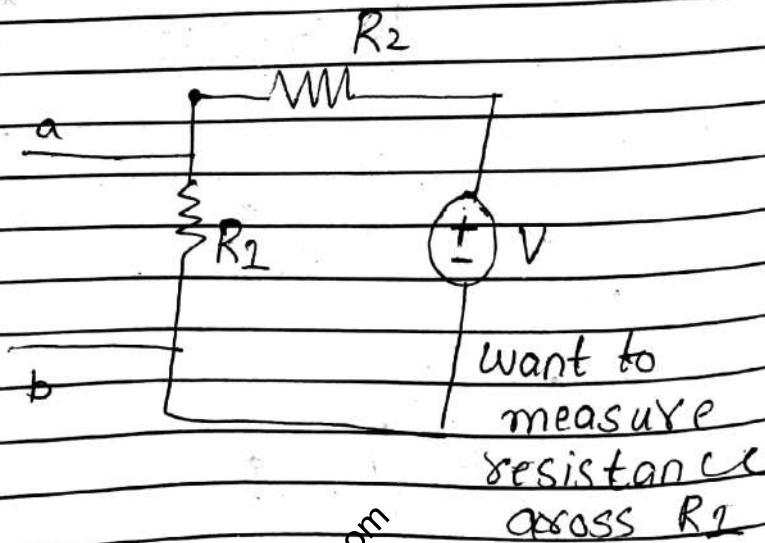
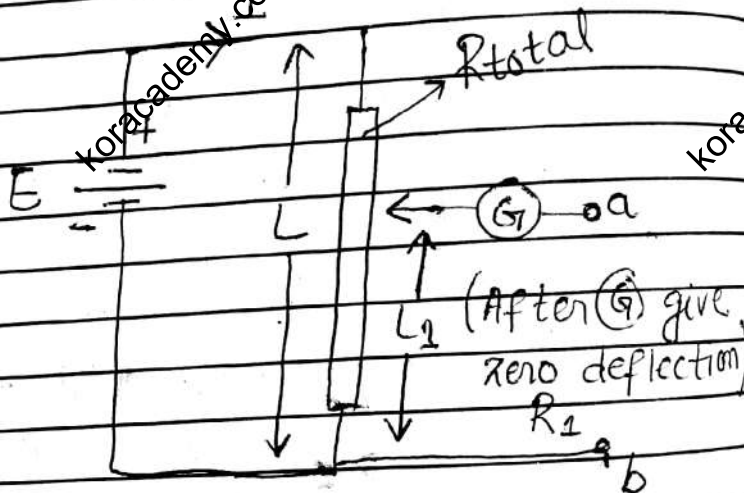
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# Calibration of DC Instrument:-

If we want to calibrate ammeter.

One of the instrument use for calibration is potentiometer.

## POTENTIOMETER:-



Date:   /  /  

We have to slide (G) across the resistive wire such that galvanometer give zero potential

⇒ voltage across galvanometer is zero

$$R_{total} = \frac{SL}{A}, \quad R_2 = \frac{SL_2}{A}$$

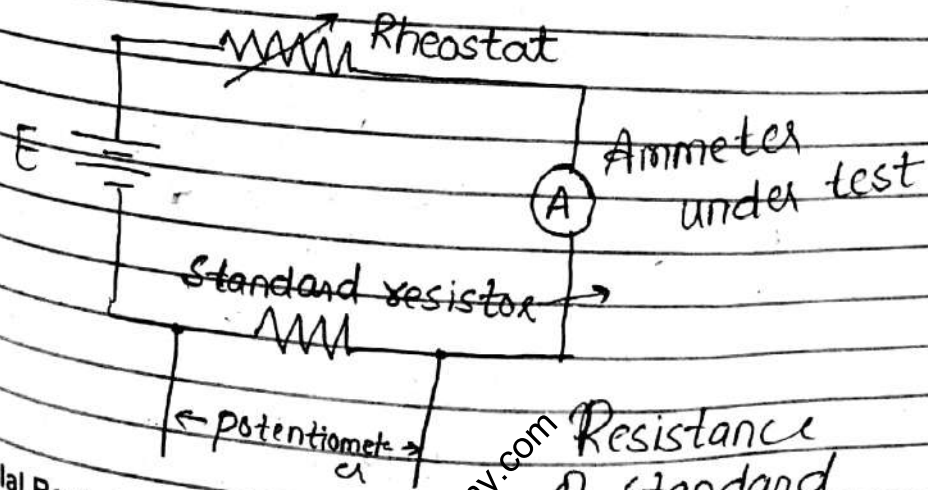
$$E = IR_{total}, \quad E_1 = IR_2$$

$$E = I \frac{SL}{A}, \quad E_1 = I \frac{SL_2}{A}$$

$$\frac{E_1}{E} = \frac{L_2}{L}$$

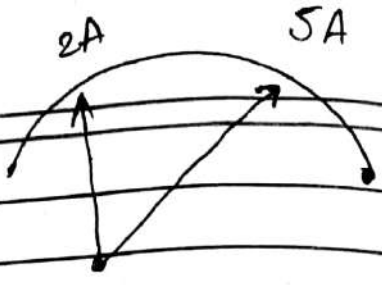
$$E_1 = \frac{L_2}{L} \cdot E$$

### Calibration of DC Ammeter:-



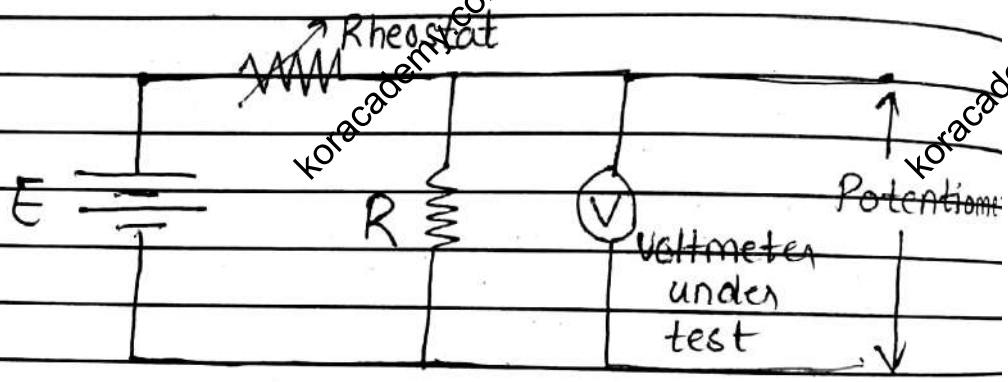
Resistance of standard resistor is known.

Date:   /  /  



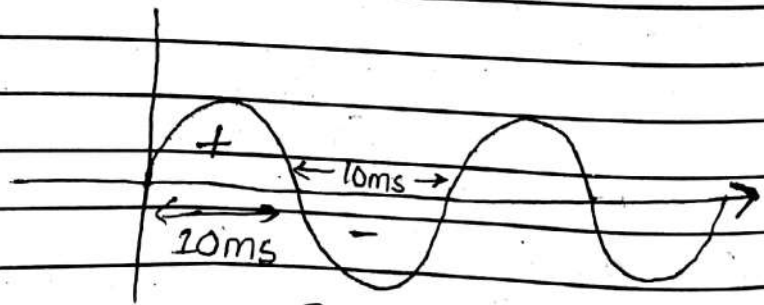
Potentiometer will give voltage across standard resistor.  
Resistance of standard resistor is known. We will divide  $\frac{V}{R} \Rightarrow$  give current in the ckt (i-e ammeter)

### Calibration of Voltmeter:-

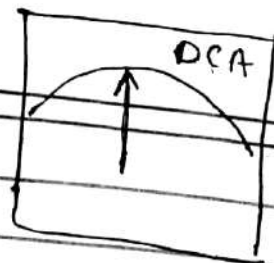


### Alternating Current indicating instrument:

$$T \propto I$$



$$f = \frac{1}{T} = \frac{1}{20\text{ms}} = 50\text{Hz}$$



# Electrodynamometer:

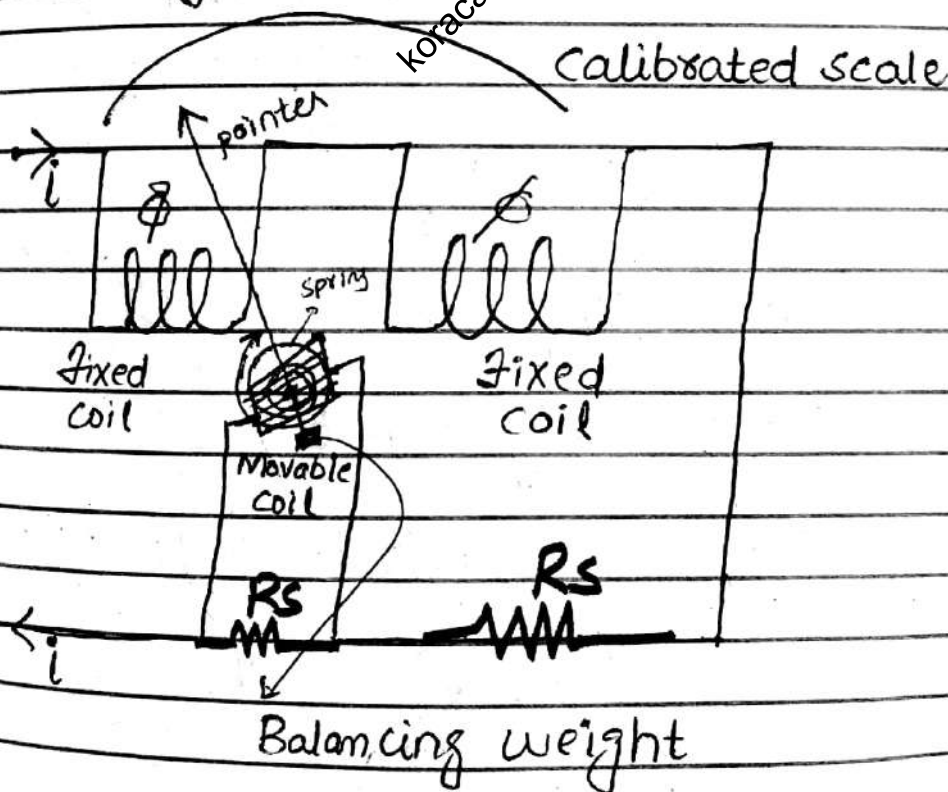
Can measure AC voltage  
 can design instrument to  
 measure power and current.

(It can measure DC as well)

Transfer Instrument:- (also Electrodyna-  
 mometer called T.I.)

Use only for power line  
 frequency (use for low  
 range frequency.)

## Electrodynamometer movement:-



When  $I$  flows fixed coil so flux  
 produce in fixed coil.  
 flux is linked with movable  
 coil

Date:   /  /  

Due to interaction of two magnetic field movable coil will rotate.

$$T \propto \phi \cdot i N$$

$N \rightarrow$  number of turns of movable coil

$$T \propto \phi i$$

$$\phi \propto i$$

$$T \propto i^2$$

If current instantaneous so Torque also instantaneous.

$$T_{\text{ins}} = K_1 i_{\text{inst}}^2$$

$$T_{\text{avg}} = \text{avg}(K_1$$

$$T_{\text{avg}} = \text{avg}(T_{\text{inst}})$$

$$T_{\text{avg}} = \text{avg}(K_1 i_{\text{inst}}^2)$$

$$T_{\text{avg}} = \frac{1}{T} \int_0^T K_1 i_{\text{inst}}^2 dt$$

$$T_{\text{avg}} = K_1 \frac{1}{T} \int_0^T i_{\text{inst}}^2 dt$$

$$I_{\text{rms}} = \sqrt{\frac{1}{T} \int_0^T i_{\text{inst}}^2 dt}$$

Date:   /  /  

$$T_{avg} = K_1 I_{rms}^2$$

With pointer we attach a spiral spring (to provide controlling torque)

$$T_c = K_2 \theta$$

The pointer will stop when both the torques becomes equal

$$T_{avg} = T_c$$

$$K_1 I_{rms}^2 = K_2 \theta$$

$$\theta = \frac{K_1 I_{rms}^2}{K_2}$$

$$\theta = K I_{rms}^2$$

$$\theta \propto I_{rms}^2$$

(Scale will be non uniform. The amount of Deflection depends on RMS value)

It is same As galvanometer for AC.

galvanometer  $\rightarrow$  for DC

T.I

If we measure DC current.

$$T \propto I^2$$

$$T = K \frac{I^2}{2}$$

$$K_2 \theta = K_1 I^2$$

$$\theta = K I^2$$

$$\theta \propto I^2$$

Disadvantage:

- 1) Scale is non uniform.
- 2) very low sensitivity. (no permanent magnet)
- 3) It has high power consumption.

Conversion to ammeter.

To increase the range add a shunt resistance across movable coil.

The conductors should be more thicker because

Range ↑

I ↑

can withstand more current



Date:   /  /  

### Conversion to voltmeter:-

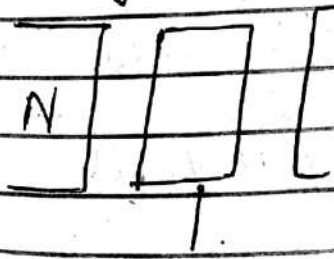
To convert it to a voltmeter add a shunt resistance in series with movable coil (—MM—)

### RECTIFIER TYPE INSTRUMENTS:

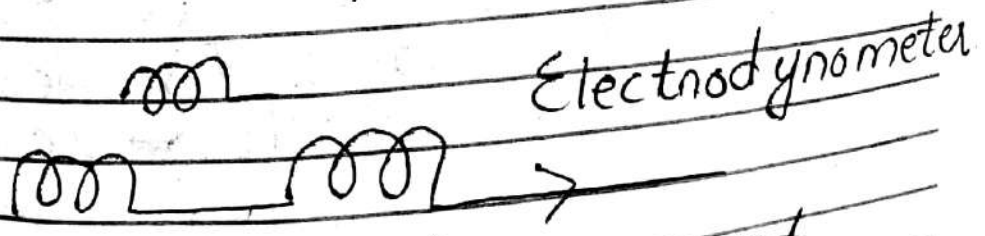
1) PMMC Instruments - D Arsonoval movement - ( $G_1$ ) DC measurement

2) Electrodynamometer EMMC ( $G_1$ ) → AC measurement.

3) Moving Iron type



S very sensitive  
But cannot be use for AC measurement.



Use this for AC measurement but is less sensitive.

Date:   /  /  

We have problems in calculating small AC currents (communication signals (small))

Rectifier type used to enhance the capability to measure small AC currents as in communication signals.

Using rectifier we use solve this problem and convert AC signal to DC and then use PMMC (which is of high sensitivity)

Signals —   
 → Power signals - 220V EMF   
 → Communication (mV,  $\mu$ V) signals

Problem: (Rectifier type instrument) you have to design ~~RIT~~ RTI for each ~~of~~ waveform

i.e sinusoidal, rectangular, triangular

Beac~~z~~ RMS value of each waveform will be different.

Date:   /  /  

we will calculate

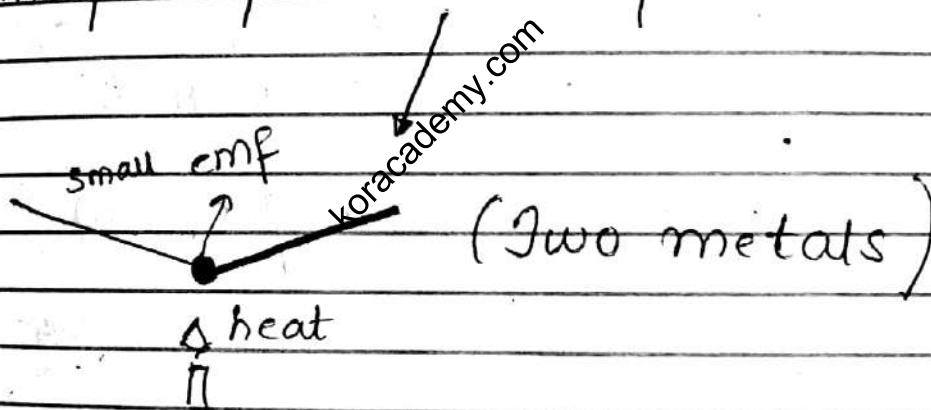
form factor for all waveforms

Form factor =

~~Typical multimed~~

~~Typical measurement circuits~~

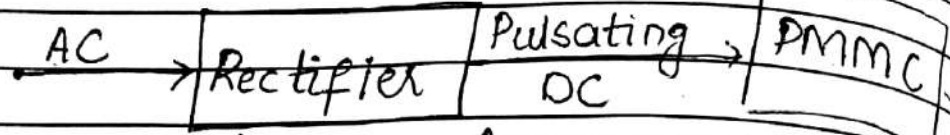
Thermo Instruments work on the principle of thermocouple.



Thermo-Instruments are used to measure small emf produced in thermocouple.

Date:   /  /  

Six January



(under measurement)

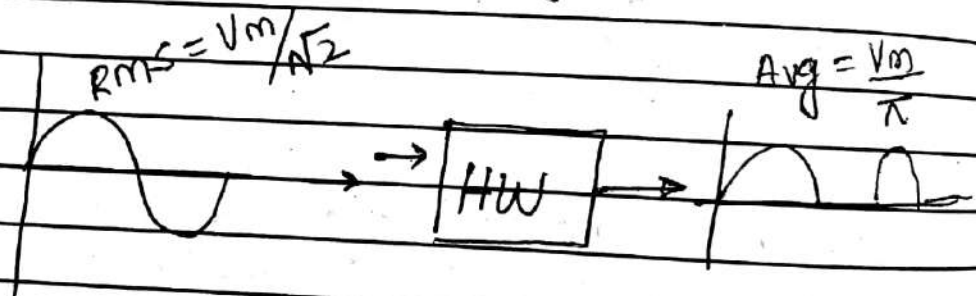
Average value = 0

Average value  $\neq 0$   
 $\Rightarrow$  having DC Components

Second solution for using AC quantities is to use a rectifier.

will respond to the average value. - and we want RMS value.

For this reading  $\times$  form factor



Form factor =  $\frac{\text{RMS value of input signal}}{\text{Average value of signal at output of rectifier}}$

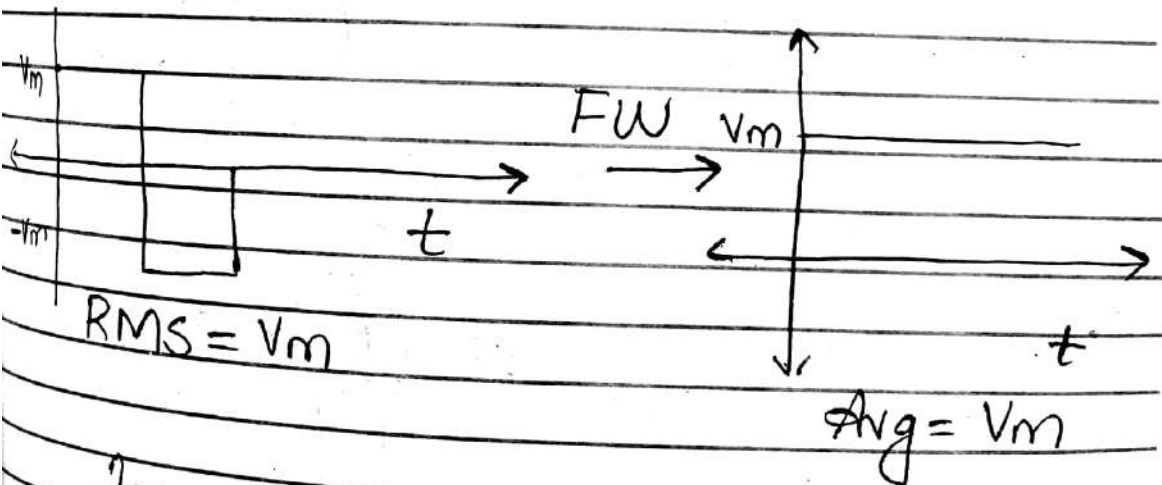
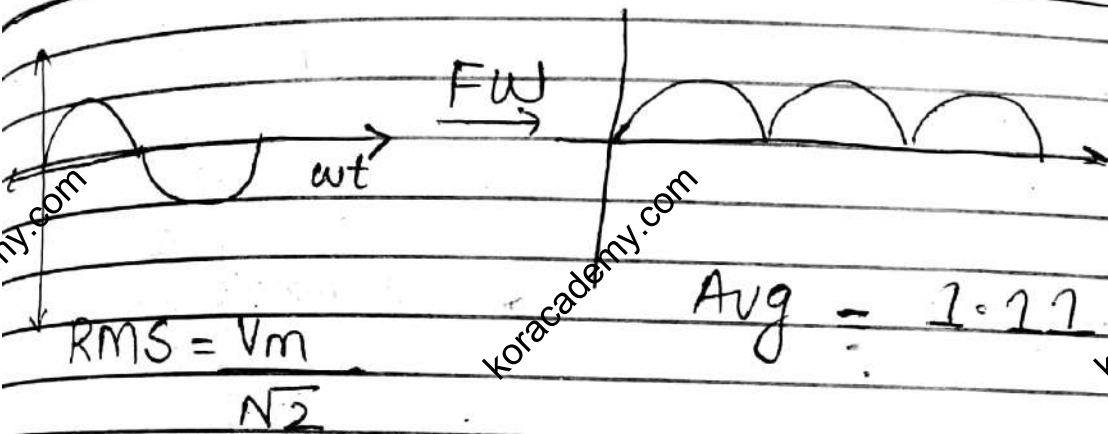
Average value of signal at output of rectifier.

Date:   /  /  

Reading  $\times$  FF

$$\text{Avg val} \times \frac{\text{RMS value}}{\text{Avg value}} = \text{RMS value}$$

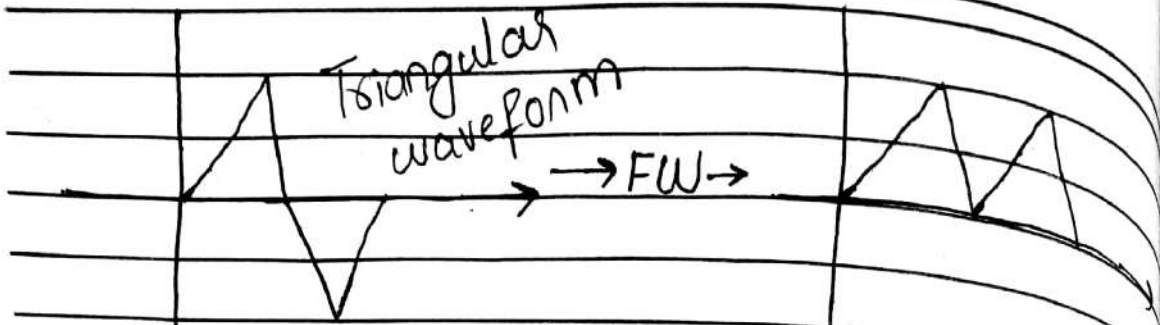
$$FF = 2.22 \text{ (Form Half Wave Rectified)}$$



Form factor = 1

For square wave we don't need to change the scale.

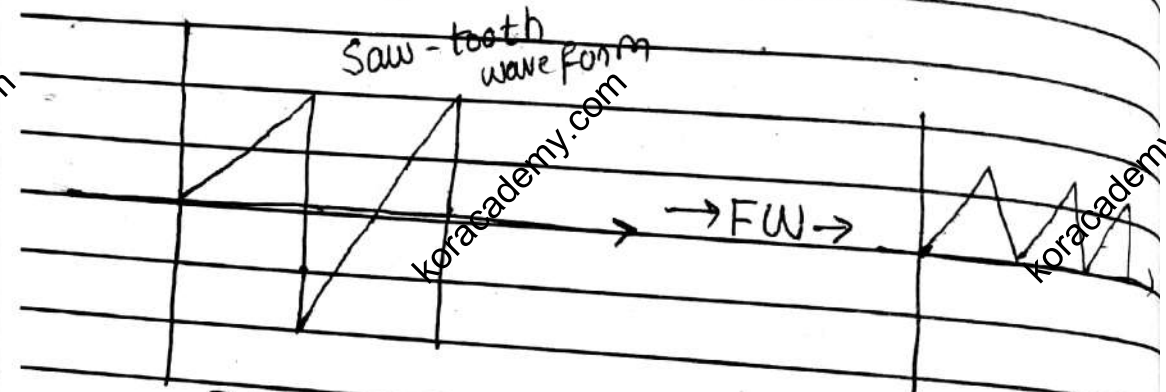
Date:   /  /  



$$RMS = \frac{V_m}{\sqrt{3}}$$

$$Avg = \frac{V_m}{2}$$

$$Form\ factor = 1.154$$



$$RMS = \frac{V_m}{\sqrt{3}}$$

$$Avg = \frac{V_m}{2}$$

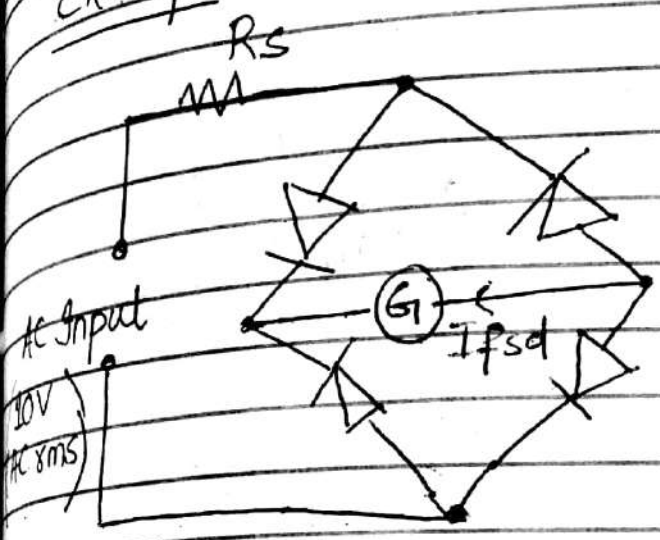
$$F \cdot F = 1.154$$

Disadvantage:- Different wavef  
Scale for different  
waveform.

Advantage: Scale is uniform  
High sensitivity

Date:   /  /  

Example:



$$R_m = 50 \Omega$$

$$I_{fsd} = 2 \text{ mA}$$

$$R_s = ?$$

10V ac  $\rightarrow$  RMS  $\rightarrow$  ~~10V~~  
 $\rightarrow$  AC full scale deflection of 10V.

The waveform is sinusoidal.

Solution:-

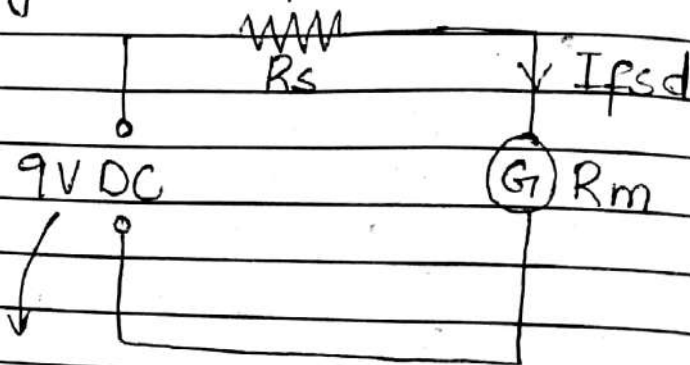
$$\text{Form factor} = \frac{E_{rms}}{E_{dc}}$$

$$E_{dc} = \frac{E_{rms}}{FF} = \frac{10}{1.11}$$

$$E_{dc} = 9 \text{ Volts.}$$

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The equivalent ckt of bridge rectifier is



For galvanometer when we apply 9V DC the ckt with is the same as bridge rectifier (when we apply 20V AC rms)

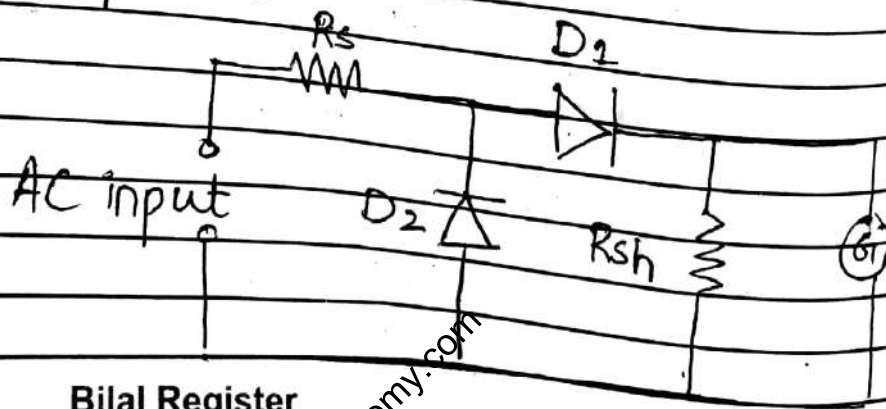
$$9 = I_{fsd} (R_s + R_m)$$

$$\frac{9}{1 \times 10^{-3}} = R_s + 50$$

$$9000 - 50 = R_s$$

$$R_s = 8950 \Omega$$

Example 4 -



Bilal Register



Date: 11 Solution:-

$$R_m = 100 \Omega$$

$$I_{fSD} = 1 \text{ mA}$$

$$R_s = 200 \Omega$$

$$R_f = 400 \Omega$$

$$R_v = \infty \Omega$$

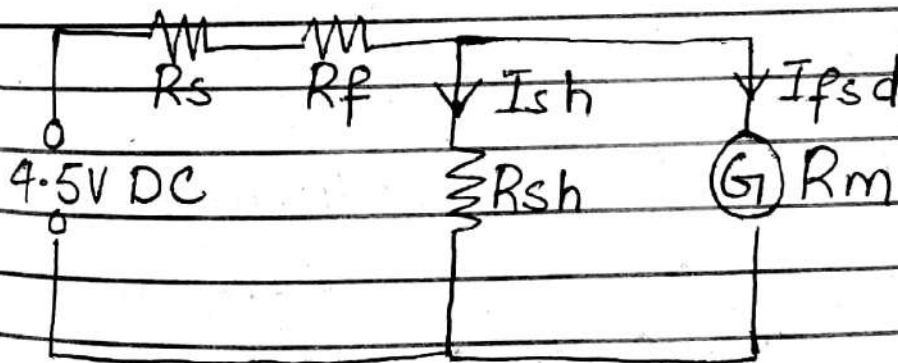
$$E_{rms} = 10 \text{ V}$$

a)  $R_s = ?$       b)  $S = ?$  (For AC range)

$$a) F \cdot F = 2.22 = \frac{E_{rms}}{E_{DC}}$$

$$E_{DC} = \frac{E_{rms}}{2.22} = \frac{10}{2.22}$$

$$E_{DC} = 4.5 \text{ volts}$$



$$I_{sh} = 1 \text{ mA}$$

$$I_t = I_{fSD} + I_{sh} = 2 \text{ mA}$$

$$4.5 = I_t (R_s + R_f + R_m \parallel R_{sh})$$

$$R_s = 1800 \Omega$$

$$b) S = \frac{R_T}{V_{ac}} = \frac{2,250}{10}$$

$$S = \frac{R_T}{f_{sd}}$$

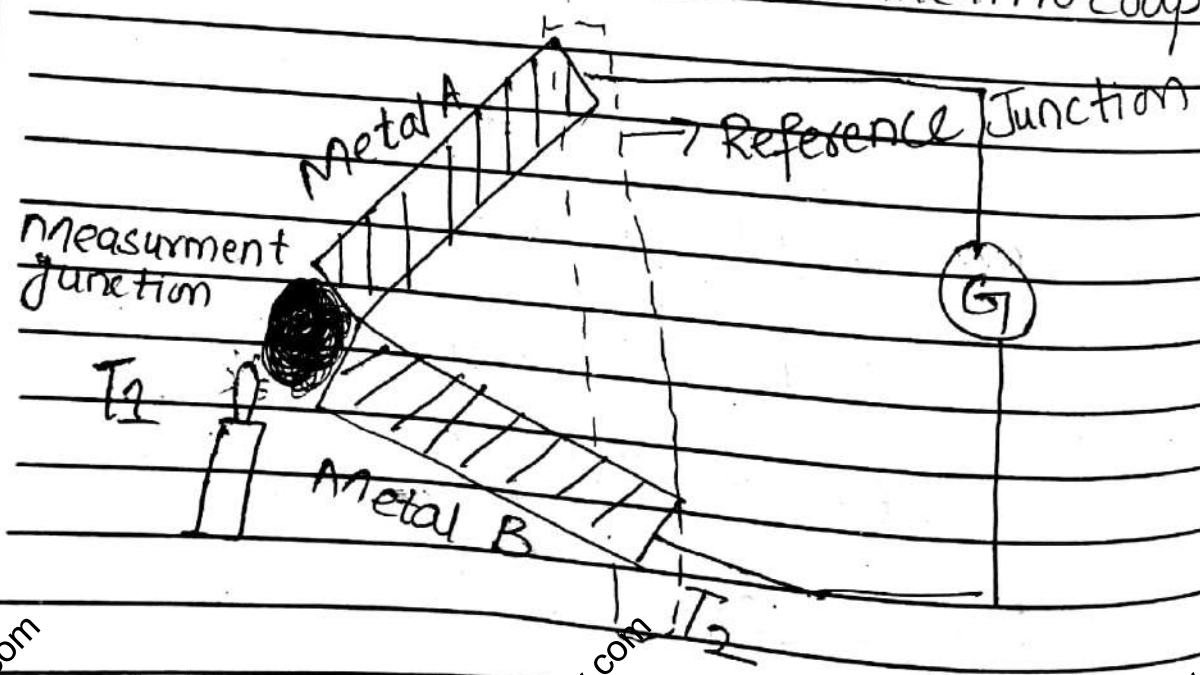
$$S = 225 \Omega/V$$

per volt resistance of  
voltmeter is  $225 \Omega/V$

### Thermoinstruments: -

We need different scale  
for different waveform  
in case of Rectifier  
type instrument therefore  
we use thermoinstruments.

Thermoinstrument uses thermocouple



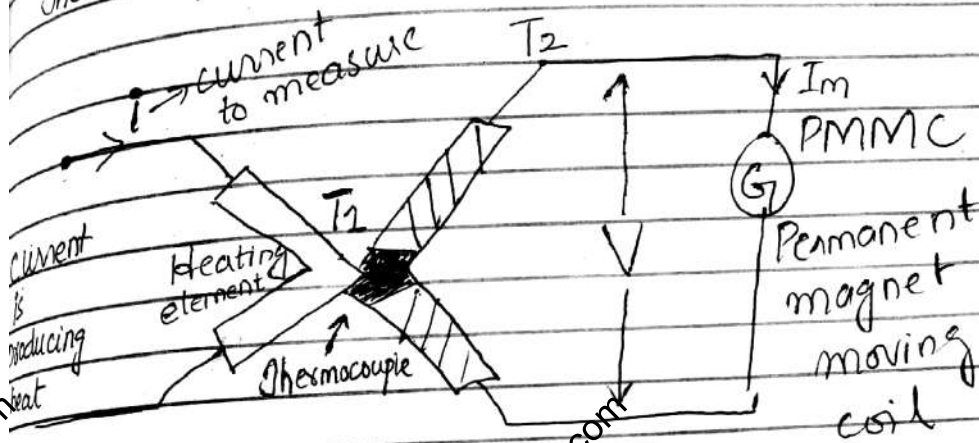
$T_1 - T_2 \propto$  potential difference

Thermocouple is the Jtn b/w two different metal

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This Effect is called Seebeck effect.

Thermocouple are temperature sensing device



$$I_m \propto V$$

$$V \propto (T_2 - T_1)$$

$$V \propto \Delta T$$

$$V = a \Delta T$$

$$I_m \propto a \Delta T$$

$$I_m = ab \Delta T$$

$$\Delta T = \frac{c I_{rms}^2 R}{R_{rms}}$$

$$I_m = abc \frac{I_{rms}^2 R}{R_{rms}}$$

$$I_m = K I_{rms}^2$$

$$I_m \propto I_{rms}^2$$

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### Watt hour meter:

### Energy meter:

$$\text{Energy} = \text{Power} \times \text{time}$$

$$E = P \times t$$

Two types of meter:

- 1) Analogue meter.
- 2) Digital meter.

1) Analogue <sup>Energy</sup> meter:-

### Single Phase Induction type Energy meter:-

→ It is integrating type instrument  
Display + Recording + addition

Babar Register

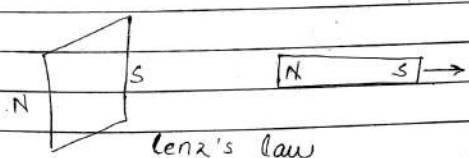
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count rotation we have registering system.  
Disc is attached to shaft.

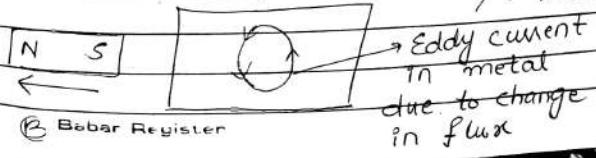
### WORKING:-

It is induction type Energy meter  
(Because phenomenon use is induction)



Lenz's law

In case of metal (circular) motion



Babar Register

Eddy current because it follows close path.

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4 Main components in Energy meter.

1) Driving System:-

Consist of voltage coil, current coil and magnetic core. The function of driving system is to produce driving torque.

2) Moving System:-

Disc, shaft, bearing. Due to driving torque produce by driving system moving system will rotate.

3) Braking System:-

To control disc motion we need braking system which is U shaped permanent magnet.

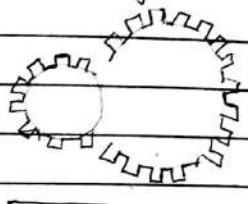
4) Registering/Counting System:-

Fourth system to count these rotation.

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Registering system is made from gears.



Size of gears will be same but connected in such a way that speed of one will be greater than another.

Working Of Energy Meter:

Voltage coil

(Highly inductor)

Current coil

I

Voltage across voltage coil is V volts.

$I_1$

$I_2$  → current flows in voltage coil

$\Phi_2$  ( $\Phi_1$  in phase with  $I_1$ )

$I_2$  lags V by  $90^\circ$  (Highly inductive)

$E_{e1}$

$I_{e2}$

Flux produce due to  $I_2$  is  $\Phi_2$

$\Phi_2 \propto I_2$

Induce Emf lags  $\phi$  by  $90^\circ$  (always)

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Due to alternating  $\phi_2$  Emf will produce in disc

$E = -N \frac{d\phi}{dt}$

$E_{e2}$  lags  $\phi_2$  by  $90^\circ$

$E_{e2}$

Power factor  $\rightarrow$  of disc

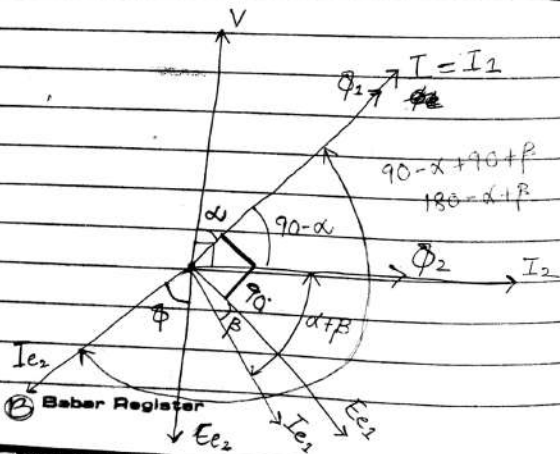
Eddy current produce due to

$I_{e2}$

Disc  $\rightarrow \beta$

Load  $\rightarrow \alpha$

Induce emf in disc lags behind  $E_{e2}$  and angle depends on impedance of disc or power factor.



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Current in disc is  $I_{e2}$   
Due to interaction of  $I_{e2}$  and  $\phi_2$  there will be a force on disc (torque will produce).

Due to interaction of  $\phi_2$  and  $I_{e2}$  torque will produce in disc.

These torques will be time varying.

$T_1 \propto I_{e2} \phi_2 \cos(\alpha + \beta)$	$T_{inst} \propto i v$ $T_{avg} \propto P$ <small>if voltage &amp; current are sinusoidal so can write power</small>
$T_2 \propto I_{e2} \phi_2 \cos(180 - \alpha + \beta)$	$T_{avg} \propto I_{e2} \cos \beta$ <small>RMS values of voltage &amp; current</small>

Viva Question:

$T_1$  &  $T_2$  are opposite in direction ( $T_1$  &  $T_2$ ) you need to verify this statement

so

Total = driving torque =  $T_d = T_1 - T_2$  torque

Babar Register

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$$T_d \propto I_e I_2 \Phi_2 \cos(\alpha + \beta) - I_e \Phi_1 \cos(180 - \alpha + \beta)$$

$$T_d \propto I V \cos(\alpha + \beta) - V I \cos(180 - \alpha + \beta)$$

$$T_d = K_1 V I [\cos(\alpha + \beta) - \cos(180 - \alpha + \beta)]$$

Home Assignment

$$T_d = 2K_1 V I \cos \alpha \cdot \cos \beta$$

$$T_d = 2K_1 \cos \beta = K_2$$

$$T_d = K_2 V I \cos \alpha$$

$$T_d = K_2 P$$

Driving torque depends on power consumed by load.

⇒ Another Eddy current will produce in disc due to  $E_{mp}$  produce. (& its cause.

Babar Register

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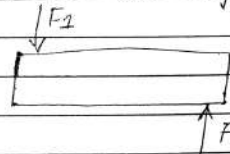
will oppose its cause) -

Due to cutting of magnetic field lines (of permanent magnet) - Emp will produce in Disc. and Eddy current will produce in disc and direction of Eddy current will be such that to oppose its cause i-e motion of disc

$T_{braking} \propto \eta$  (Speed of disc)  
rev/sec  
rev/min  
rev/hr.

$$T_b = K_3 \eta$$

Point of action of these torques  $T_d$  and  $T_b$  are different.



$T_d$  and  $T_b$  are of same magnitude but their point of action is different. So disc will move

$\Sigma F = 0$   
 $a = 0$   
uniform velocity

Babar Register

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with uniform speed.

$$\tau_b = \tau_d$$

Disc will rotate with a uniform speed.

$$K_3 \omega = K_2 P$$

$$K_3 \omega t = K_2 P t$$

$$K_3 N = K_2 E$$

$$N = \frac{K_2 E}{K_3}$$

$$N = KE$$

$$N \propto E$$

$$K = \frac{N}{E} \left( \frac{\text{rev}}{\text{Kwh}} \right)$$

$$K = 1500$$

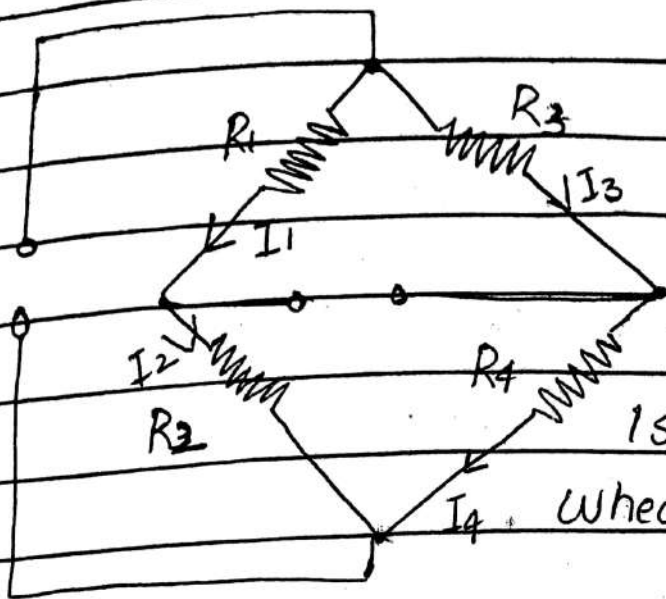


## LECTURE #02

### BRIDGE MEASUREMENT:

Every bridge has

- 1) Input voltage source (ac, dc)
- 2) Output detector (G, buzzer, Electron eye etc)
- 3) Four sets of arms.
- 4) Checked for balance/unbalance conditions
- 5) Proper ~~arms~~ balancing of arms.
- 6) For solving we use KVL and KCL.



As if bridge consist of all resistors the bridge is called wheat stone bridge

$R_4$  is unknown resistance.

At two pts we apply source. (Rem two

At two pts we apply galvanometer. (connect).

At balance condition

$$I_1 = I_2 \text{ and } I_3 = I_4$$

$$I_3 R_3 = I_1 R_1 \text{ and } I_4 R_4 = I_2 R_2$$

Unknown

resistor will be the part of that arm which consist of variable resistor

Wheatstone bridge can be use for measuring

- 1) Inductance
- 2) Capacitance
- 2) Conductance
- 3) Admittance.

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If Galvanometer current is zero (in balance condition)

$$I_1 = I_3 = \frac{E}{R_2 + R_3}$$

$$I_2 = I_4 = \frac{E}{R_2 + R_4}$$

$$R_2 R_4 = R_2 R_3$$

We have limiting resistor it can withstand a certain amount of voltage & current. We should know power handling capability of bridge and should not go beyond that.

We make galvanometer bridge of same material to avoid thermal emf.

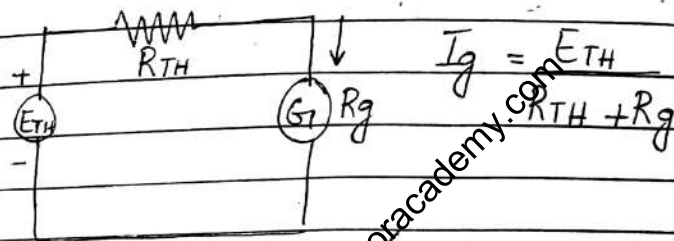
Errors may be reduced by using a Kelvin bridge.

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### Thevenin Equivalent circuit:-

This helps to select the desired galvanometer (of particular sensitivity).

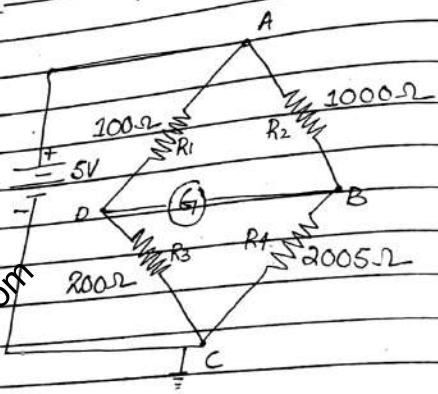


$$I_g = \frac{E_{TH}}{R_{TH} + R_g} \quad (\text{so by})$$

Knowing value of  $I_g$  we can select a particular galvanometer for our bridge.

$I_g \rightarrow$  Minimum current which is to be detected

Example 5-2



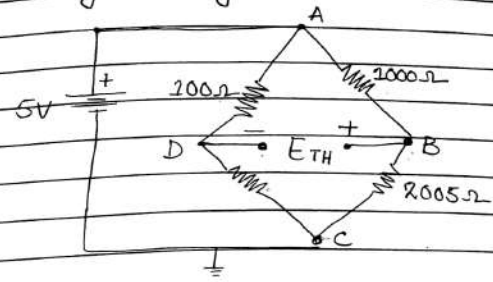
Bridge will be balance  
 $R_2 R_4 = R_2 R_3$   
 In this case bridge is not  
 in balance condition.

$S = 10 \text{ m m} / \mu\text{A} \Rightarrow S = \frac{\Delta \text{output}}{\Delta \text{input}}$

$R_m = 100 \Omega$

$D = ?$

Solving it by thevenin theorem:-

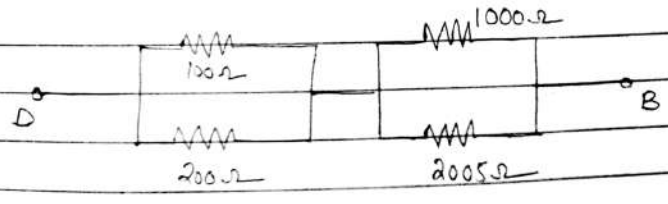
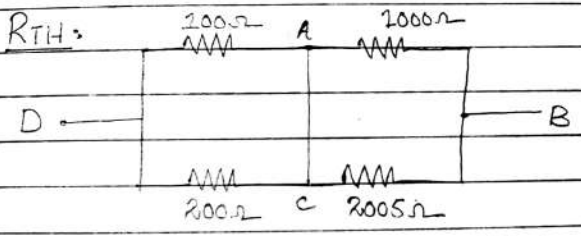


$E_{TH} = -$

$E_{TH} = E_B - E_D$   
 $E_{TH} = \frac{5 \times 2005}{1000 + 2005} - \frac{5 \times 200}{100 + 200}$

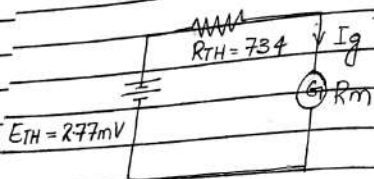
$E_{TH} = 2.77 \text{ mV}$

$R_{TH} =$



$$R_{TH} = 100 // 200 + 1000 // 200.5$$

$$R_{TH} = 734 \Omega$$



NOTE:

We cannot use wheatstone for measuring resistance less than  $1 \Omega$  and greater than few Mega ohms.

$$I_g = \frac{E_{TH}}{R_{TH} + R_m}$$

$$I_g = \frac{277 \times 10^{-3}}{734 + 10.0}$$

$$I_g = 3.32 \text{ mA}$$

$$D = I_g \times S$$

$$= 332 \times 10 = 332 \text{ mm}$$

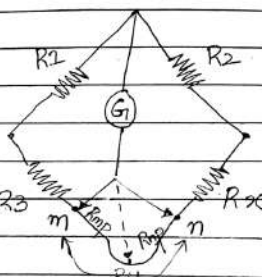
$$D = 332 \text{ mm}$$

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If resistance is less than  $1 \Omega$  we cannot neglect resistance of wires & leads.

Effect of connecting leads:  
 $R_x \ll 1 \Omega$ :



$$R_1 R_x = R_2 R_3$$

$$R_x' = R_x + R_y \quad (\text{If lead is connected to } m)$$

Then  $R_y$  is added  $R_x$ . Indication will be greater than  $R_x$ .

If Galvanometer is connected to pt m. The actual value of  $R_3$  is  $R_3 + R_y$  but we take  $R_3$  so the indication (value of  $R_x$ ) will be less than  $R_x$ .

Bebar Register

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If galvanometer is connected to point P.

Balanced:-

$$R_1(R_x + R_{gp}) = R_2(R_3 + R_{gp})$$

$$R_1 R_x + R_1 R_{gp} = R_2 R_3 + R_2 R_{gp}$$

$$R_1 R_x = R_2 R_3 + R_2 R_{gp} - R_1 R_{gp} \quad (1)$$

We have to choose point such as:-

$$\frac{R_{gp}}{R_1} = \frac{R_2}{R_1}$$

$$R_2 R_{gp} = R_1 R_{gp}$$

If this condition is satisfied so we can use wheat stone bridge for low resistances. So eq (1) will become

$$R_1 R_x = R_2 R_3$$

Babar Register

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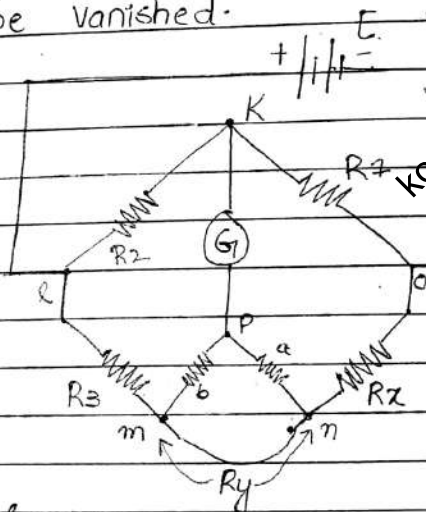
Day

For selecting point P we have Kelvin Bridge:

We have to choose a and b resistors such that we get point P. and

$$\frac{a}{b} = \frac{R_2}{R_3}$$

Effect of lead resistance will be vanished.



Balanced:

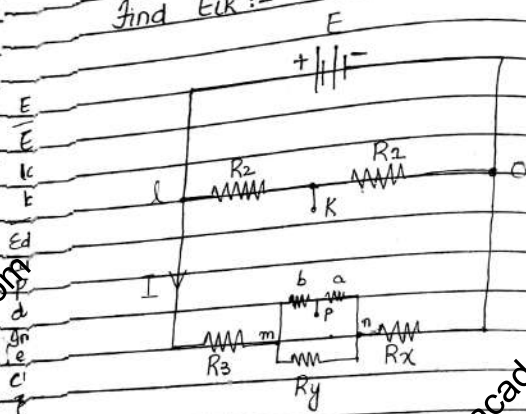
$$-E_k = -E_p$$

$$E_l - E_k = E_l - E_p$$

$$E_k = E_p \quad (2)$$

Babar Register

Find  $E_{K}$  :-



$$E_K = E \times \frac{R_2}{R_1 + R_2} \quad \text{--- (3)}$$

$$E = I \times (R_3 + (a+b) \parallel R_y + R_x) \quad \text{--- (4)}$$

$$E_K = \frac{R_2}{R_1 + R_2} \times I \times (R_3 + (a+b) \parallel R_y + R_x) \quad \text{--- (5)}$$

$E_{xp}$  :-

$$E_{xp} = IR_3 + E_{mp} \quad \text{--- (6)}$$

Bebar Register

$$E_{mp} = E_{mn} \times \frac{b}{a+b} \quad \text{--- (7)}$$

$$E_{mn} = I \times (a+b) \parallel R_y \quad \text{--- (8)}$$

$$E_{mp} = I \times \frac{(a+b) R_y \times b}{a+b+R_y} \quad \text{--- (9)}$$

$$E_{mp} = I \times \frac{b R_y}{a+b+R_y} \quad \text{--- (9)}$$

Put eq (9) in eq (6)

$$E_{xp} = I \left( R_3 + \frac{b R_y}{a+b+R_y} \right) \quad \text{--- (10)}$$

$$E_K = E_{xp}$$

$$\frac{R_2}{R_1 + R_2} \times I \times (R_3 + (a+b) \parallel R_y + R_x)$$

$$= I \times (R_3 + \frac{b R_y}{a+b+R_y})$$

$$\frac{R_3 + a R_y}{a+b+R_y} + \frac{b R_y}{a+b+R_y} + R_x = \frac{R_1 + R_2}{R_2} \times \frac{R_3 + b R_y}{a+b+R_y}$$

Bebar Register

$$R_3 + aR_1 + bR_2 + R_x = \frac{(R_1 + 1)}{R_2} \frac{R_3 + bR_2}{a + b + R_2}$$

$$R_3 + aR_1 + bR_2 + R_x = \frac{R_2 R_3 + R_1 \cdot bR_2}{R_2 (a + b + R_2)}$$

$$+ R_3 + bR_2$$

$$R_x = \frac{R_2 R_3 + R_1 \cdot bR_2}{R_2 (a + b + R_2)} - \frac{b a R_1}{b (a + b + R_2)}$$

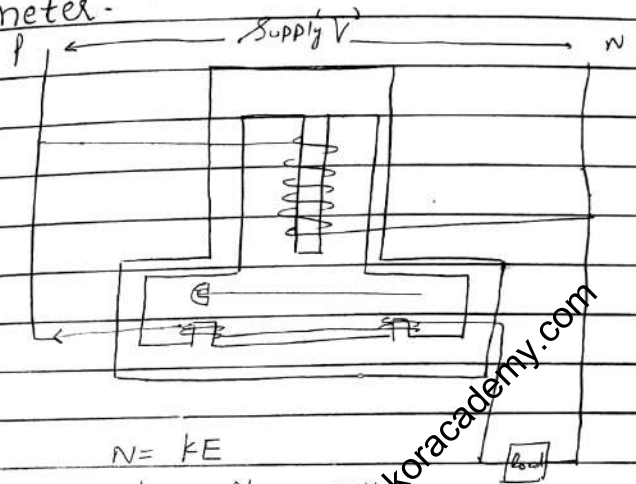
$$R_x = \frac{R_2 R_3 + bR_2}{R_2 (a + b + R_2)} \left( \frac{R_1}{R_2} \frac{a}{b} \right)$$

$$\frac{a}{b} = \frac{R_1}{R_2}$$

$$R_x = \frac{R_2 R_3}{R_2}$$

Lab # 09: -

To find the meter constant of a single phase analog Energy meter.



$$N = kE$$

$$k = \frac{N}{E} \frac{2\pi V}{kWh}$$

Voltage coil is highly inductive its resistance is almost zero.

Disc is made from aluminium.

Registering system counts no. of rotations of disc.



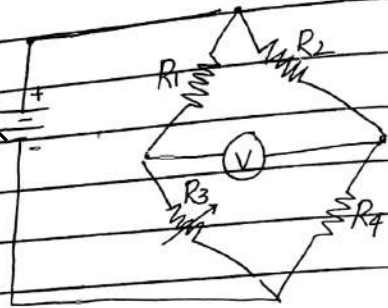
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Clamp

Lab # 10:-

To measure unknown resistance using wheatstone bridge



$$R_1 R_4 = R_2 R_3$$

$$R_4 = \frac{R_2 R_3}{R_1}$$

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### LECTURE # 03

(When we use inductor and capacitor)

1 Source → AC

- ↳ Power line frequency (50-60 Hz)
- ↳ Radio frequency.

2) Detector:-

- ↳ Buzzer
- ↳ Headphone
- ↳ Electron gun / eye
- ↳ Amplifier

3) 4 Arms

- ↳ Resistor
- ↳ Capacitor
- ↳ Inductor.

4) Basic principle for Balanced condition

Opposite

In bridge Capacitor - resistor & Inductor - resistor

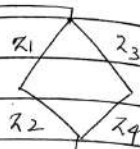
is possible

B Babar Register

Date: / / Day: \_\_\_\_\_  
 we will deal impedances as phasors.

$$\bar{Z}_1 = Z_1 / \theta_1$$

$$I_1 = \frac{E}{Z_1 + Z_2}$$



$$I_2 = \frac{E}{Z_3 + Z_4}$$

Under balanced condition  
 $Z_1 Z_4 = Z_2 Z_3$   
 When using admittances

$$(Z_1 / \theta_1)(Z_4 / \theta_4) = (Z_2 / \theta_2)(Z_3 / \theta_3)$$

$$Z_1 Z_4 / \theta_1 + \theta_4 = Z_2 Z_3 / \theta_2 + \theta_3$$

$$\Rightarrow Z_1 Z_4 = Z_2 Z_3$$

$$\Rightarrow \theta_1 + \theta_4 = \theta_2 + \theta_3$$

Exple 5.3 :-  
 Exple 5.4 :-

### MAXWELL BRIDGE:

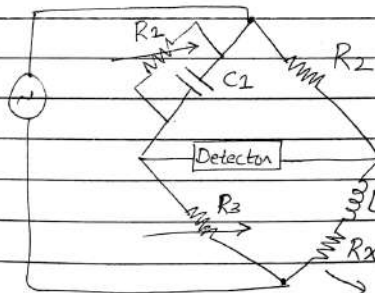
It is use to find out the value of unknown inductance.  
 Maxwell Bridge

Maxwell inductance bridge

$$Z_1 = R_1 + j\omega L_1$$

Maxwell inductance capacitance bridge

$$Z_1 = R_1 + \frac{1}{j\omega C_1}$$



Maxwell bridge for inductance measurements.

All other are known.

Unknown coil

$$R_x = \frac{R_2 R_3}{R_1}$$

$$L_x = R_2 R_3 C_1$$

### Findings/Conclusion:-

- 1) There is no role of frequency in the  $L_x$  and  $R_x$ .
- 2) We can calibrate inductance using resistances.
- 3) No inductive losses.

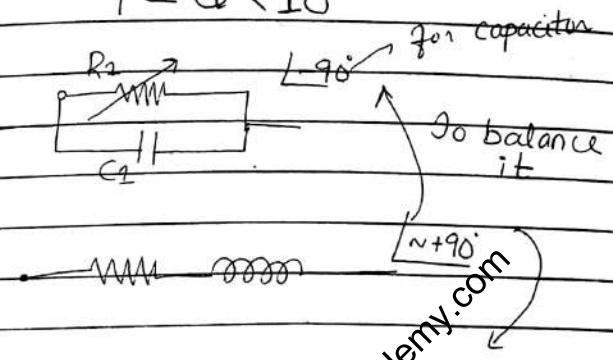
### Limitations:-

To find out which coil is of better quality we deal with Q-factor (Quality factor)

↑ Q-factor = Energy stored in coil  
 ↓ Energy dissipated

We can use maxwell bridge for finding  $L_x$  and  $R_x$  of low quality.

$$1 < Q < 10$$



One solution is to balance +90 of inductor to -90 of capacitor

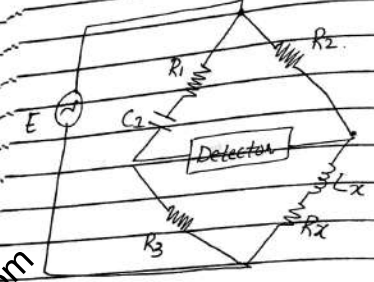
- 1) To have a large resistance.
- 2) To vary capacitance of capacitor (variable capacitor) - [we should be having a good capacitor which is very expensive]

We cannot use maxwell bridge for low Q-

We can use maxwell bridge for medium Q.

Variable capacitors are expensive

### HAY BRIDGE



$$Z_1 = R_1 + \frac{1}{j\omega C_2}$$

$$Z_1 = R_1 - \frac{j}{\omega C_2} \quad (H/w)$$

$$R_x = \frac{\omega^2 C_2^2 R_2 R_3}{1 + \omega^2 C_2^2 R_2^2}$$

$$L_x = \frac{R_2 R_3 C_2}{1 + \omega^2 C_2^2 R_2^2}$$

Frequency of the source must be accurately known.

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Q-factor =  $\frac{\text{Energy stored in coil}}{\text{Energy dissipated}}$

$$= \frac{X_L}{R}$$

$$\tan \theta_L = \frac{X_L}{R} = \omega L_x = Q$$

$$\tan \theta_L = \tan \theta_C \text{ on } Q = 1$$

$$\tan \theta_L = \tan \theta_C \text{ on } Q = 1$$

$$\tan \theta_C = \frac{X_C}{R}$$

$$L_x = \frac{R_2 R_3 C_2}{1 + (1/Q)^2}$$

$Q > 10$

e.g.  $Q = 100$

$$L_x = \frac{R_2 R_3 C_2}{1 + (1/100)^2}$$

→ Neglecting  $(1/100)^2$

$$L_x = R_2 R_3 C_2$$

For High Quality coil we use hay bridge

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### Guarded Wheatstone Bridge:

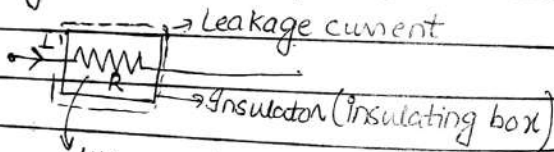
We can use wheatstone bridge upto few megaohms.

Problem if resistance is too much.

i)  $I \downarrow$  (Current will be too much less as galvanometer

will show no deflection) Sensitivity of galvanometer is the problem - we have to increase sensitivity of galvanometer.

2) Leakage current problem:-

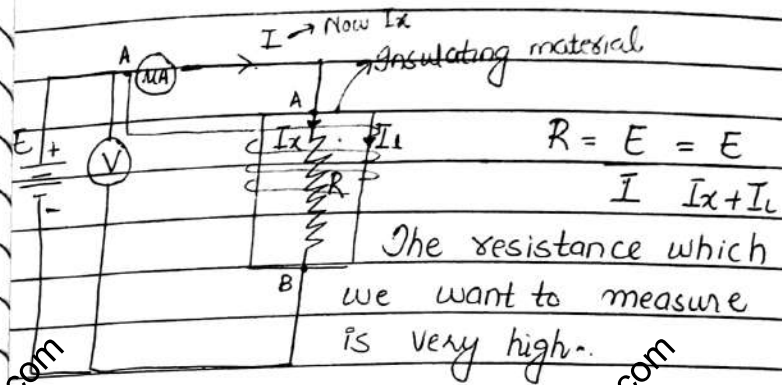


We want to measure the resistance of high resistor. Due to Temp, humidity leakage current will affect

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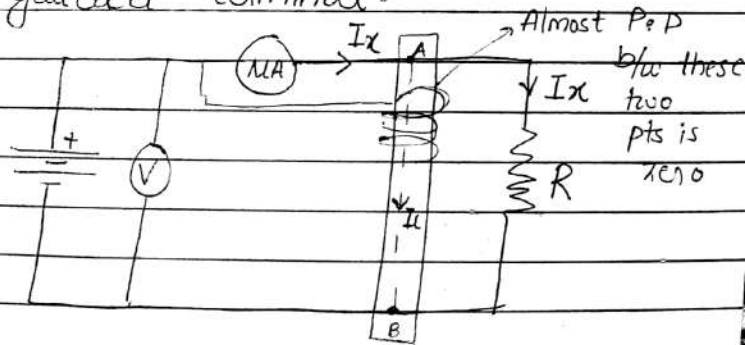
Leakage current will cause measurement errors

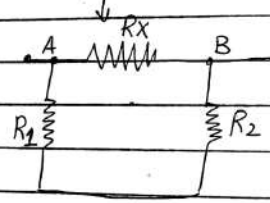
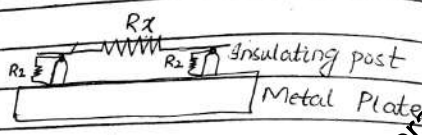
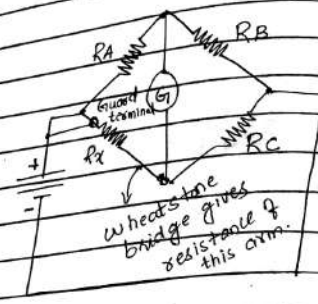


$$R_{\text{actual}} = \frac{E}{I_x}$$

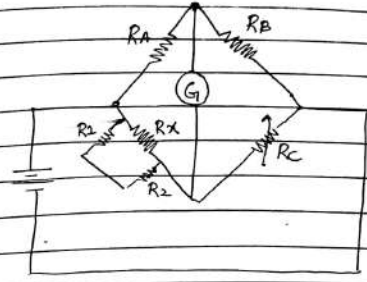
If increase R  $I_L$  will also increase and the error will increase.

A → This terminal is called as guarded terminal.

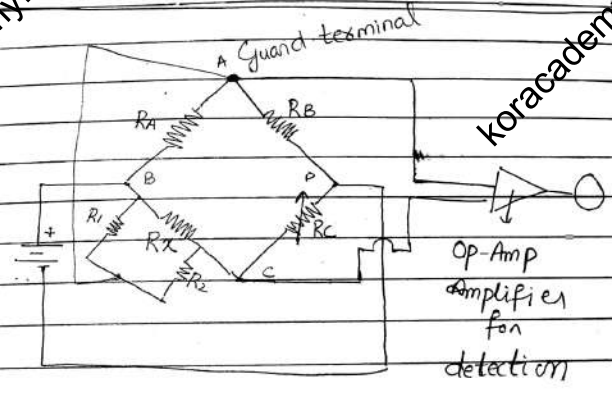




$$R_X // (R_2 + R_2)$$



$$R_X = \frac{R_A R_C}{R_B} = R_X // (R_2 + R_2)$$



(m<sub>1</sub>) R<sub>2</sub> is connected in parallel with R<sub>A</sub> (R<sub>2</sub>)

$$R_2 // R_A \equiv R_A$$

(m<sub>2</sub>) R<sub>2</sub> is connected in parallel

$$R_2 // R_m \approx R_m$$

Exple:-

$$R_x = 200 M\Omega$$

actual

$$R_2 = R_2 = 200 M\Omega$$

So find % Error

$$\text{Measured } R_x = R_x // (R_1 + R_2)$$

$$= 100 // 200$$

$$= 67 M\Omega$$

$$\% \text{ Error} = \frac{\text{Measured} - \text{Actual}}{\text{Actual}}$$

$$= 33\%$$

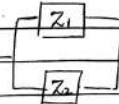
We prefer Hay bridge for Quality factor  $> 10$

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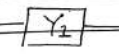


$$Z_1 + Z_2$$



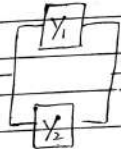
$$\frac{Z_1 Z_2}{Z_1 + Z_2}$$

$$\frac{Z_1 Z_2}{Z_1 + Z_2}$$



$$\frac{Y_1 Y_2}{Y_1 + Y_2}$$

$$\frac{Y_1 Y_2}{Y_1 + Y_2}$$



$$Y_1 + Y_2$$

$$Z = R + jX$$

R = Resistance

X → Reactance

$$X_L = j\omega L$$

$$X_C = \frac{-j}{\omega L}$$

$$Y = G + jB$$

$$G = \text{Conductance} \rightarrow G = \frac{1}{R}$$

$$B = \text{susceptance} \rightarrow B = \frac{1}{X}$$

Date: \_\_\_\_\_ **LECTURE # 04**

**Instrument Transformers:**

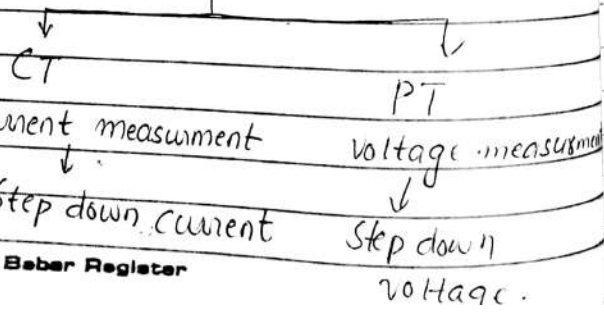
CT is a type of instrument transformer.

These are called instrument transformers because they are used with instruments (ammeter, voltmeter, wattmeter, and energy meter).

We cannot measure 100's of ampere and large voltage with ammeter and voltmeter.

To increase their range we use instrument transformer.

**Instrument transformer**



Bebar Register

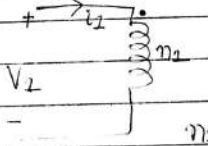
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Two important functions of instrument transformer:-

- 1) They extend the range of measuring instruments.
- 2) They provide isolation.
- 3) When we use instrument transformer to increase range so losses will be low (Low power consumption).

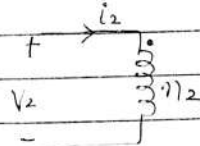
**IDEAL TRANSFORMER:**

- 1) It provides isolation (It provides safety)

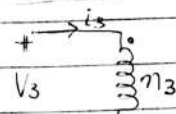


If all currents are moving towards dot

$$n_1 i_1 + n_2 i_2 + n_3 i_3 = 0 \quad \text{--- (1)}$$



$$\frac{V_1}{n_1} = \frac{V_2}{n_2} = \frac{V_3}{n_3} \quad \text{--- (2)}$$

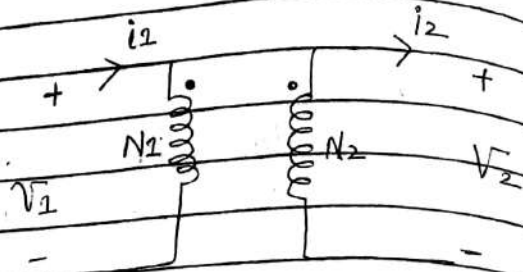


Bebar Register



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Using eq 1

$$N_1 i_1 + N_2 (-i_2) = 0$$

$$N_1 i_1 = N_2 i_2$$

$N_1$	$=$	$i_2$
$N_2$		$i_1$

Using second relationship :-

$$\frac{V_1}{N_1} = \frac{V_2}{N_2}$$

$V_1$	$=$	$N_1$
$V_2$		$N_2$

Current transformer has to step down the current.

Babar Register

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CT:- It may be use with ammeter so we decreases I and then measure it and then multiply it with the number of turns to get the actual current.

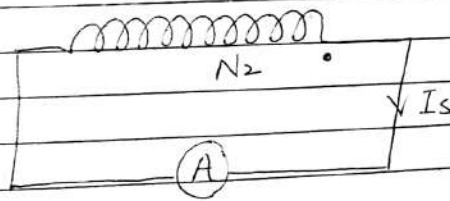
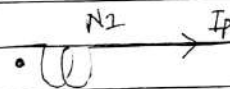
In current transformer

$$I_2 < I_1 \rightarrow \text{always}$$

$$N_2 > N_1$$

If  $N_1 = 1$  (Primary coil turn ratio = 1)

Bar Primary means number of turns at primary = 1



$0 \leq I_s \leq 5A$  (should be in this range)

Nr

$$N_1 I_1 = N_2 I_2$$

$$I_1 = \frac{N_2}{N_1} I_2$$

Babar Register

Question:-

We want to measure current from range of 0-500A but we have an ammeter whose range is 5A so find turns ratio  $\left(\frac{N_2}{N_1}\right)$  of C.T

$$\frac{N_2}{N_1} = 100$$

Viva Question

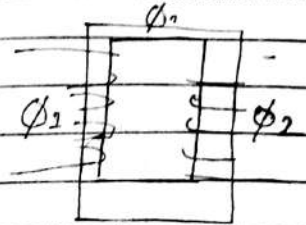
Why secondary winding of a C.T should never be open circuited?

Ans: It is basically a step up transformer

$$\begin{aligned} \text{becoz } N_2 > N_1 \\ V_2 > V_1 \end{aligned}$$

It. A high voltage will damage the insulation (painting)

$$E_s = -N_2 \frac{d\phi}{dt}$$



Load is that thing connected at output of transformer. It is mentioned in Volt-Ampere.

$$500A / 5A$$

10VA

5p20

Error which comes is 5%.

20 means CT can carry 20 times more (higher) than rated values.

Equivalent ckt of CT:-

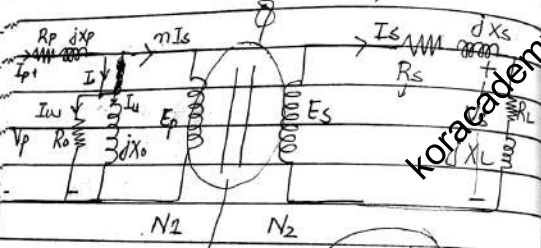
Ideal transformer is that in which losses is equal to zero

$$I/P \text{ power} = O/P \text{ power}$$

Losses in Practical T/F :-  
 → Leakage flux  
 → Electrical losses in coil  
 → Losses in core.

Practical Equivalent Ckt of T/F :-

Ideal T/F is a part of practical T/F.



$$\eta = \frac{N_2}{N_1}$$

- two lines // → Iron core
- / → Ferromagnetic core
- no lines → Air core.

$R_s$  → Electrical losses in secondary  
 $X_s$  → leakage flux in secondary.

$jX_o$  →  $I_o$  represent mutual inductance.

$V_p$  = Input Primary voltage  
 $I_p$  = Input current

$R_p$  = Primary winding resistance. and it represent the internal resistance of copper which is use in primary side.

$X_p$  = Primary winding leakage reactance. Also called parasitic reactance. It is responsible for leakage flux.

$R_o$  is resistance of the core it is responsible for core losses or iron losses.

$X_o$  ⇒ Magnetizing reactance of core. Magnetizing inductance of core. It is responsible for producing that working flux.

$I_s \Rightarrow$  Secondary winding current.

$R_s \Rightarrow$  Secondary winding resistance.  
Conduction losses in S-Side.

$X_s \Rightarrow$  It is called secondary winding leakage reactance

$+jX_L$  (Inductive load or burden)

$E_p \Rightarrow$  Induced primary voltage.

$E_s \Rightarrow$  Induced secondary voltage.  
Also called no load secondary voltage.

$V_s =$  Secondary voltage.

$I_0 =$  No load <sup>primary</sup> current

$I_p = I_0$  As  $I_s = 0$

$nI_s = 0$

$R_o$  &  $I_w$  is core loss component

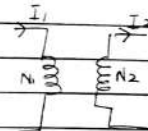
$I_m$  is magnetizing current

$\phi =$  Core flux or working flux of transformer.

$n = \frac{N_2}{N_1} =$  Nominal ratio

Ideally

$n = \frac{I_1}{I_2} = \frac{I_p}{I_s} = \frac{N_2}{N_1}$



It is only valid for ideal T/F not for practical T/F.

$\delta =$  angle b/w  $I_s$  and  $E_s$

$\delta = \tan^{-1} \left( \frac{X_L + X_s}{R_L + R_s} \right)$

$I_p = I_s + nI_s$

$\frac{I_p}{I_s} > n$

This error is called

Bobar Register as ratio error

Ideally

$I_p = nI_s$

$\frac{I_p}{I_s} = n$

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This error is due to  $I_0$ .

Ideally

Practically

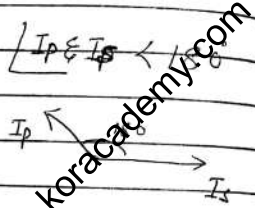
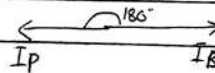
$$1) \frac{I_p}{I_s} = n \Rightarrow I_p = n I_s$$

$$I_p > n I_s$$

$$\frac{I_p}{I_s} > n \text{ (Ratio Error)}$$

Angle b/w  $I_p$  &  $I_s$  is  $180^\circ$  (According to Lenz's law)

$$\angle I_p \& I_s = 180^\circ$$



This Error is also due to  $I_0$  and is called Phase angle Error.

$I_w$  is in-phase with  $E_p$  As across  $E_p$  we have  $R_0$  and current in  $R_0$  is  $I_w$ .

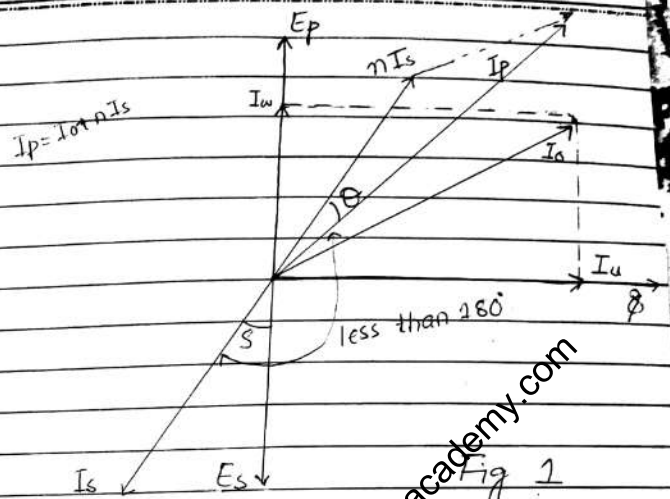
$I_s$  lags behind  $E_s$  by angle of  $\delta$  (sigma)

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Formula to find Actual Ratio:- Actual Ratio is represented by  $R$ .

$$R = n + \frac{I_w \cos \delta + I_u \sin \delta}{I_s}$$

$$R = \frac{I_p}{I_s} \text{ Actual ratio.}$$

$$\% \text{ Ratio Error} = \frac{n - R}{R} \times 100$$

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If Burden is resistive (load is resistive)  
 so  $\delta$  is almost zero.

$$R = \frac{n + I_w}{I_s}$$

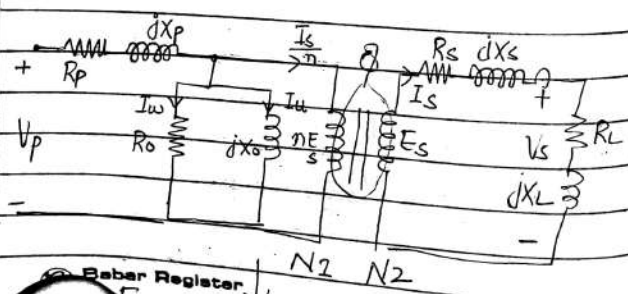
Phase angle Error ( $\theta$ ):-

$$\theta = \frac{I_w \cos \delta - I_s \sin \delta \times 180}{n I_s \pi}$$

### POTENTIAL TRANSFORMER (PT):

Equivalent ckt of PT is same as CT. (as mentioned above)

We use it to increase the range of voltmeter.



Babar Register  
 For all transformers

$$n = \frac{N_1}{N_2} \quad n > 1$$

$$\frac{E_p}{E_s} = n \quad \text{Ideally T/F}$$

In Practical transformer  
 $\frac{V_p}{V_s} > n$  (Ratio Error).

$$R = n + \frac{I_s}{n} (R_p \cos \delta + X_p \sin \delta) + I_w R_p + I_w X_p$$

$$\theta = \frac{I_s}{n} (X_p \cos \delta - R_p \sin \delta) + I_w X_p - I_w R_p$$

Actual phase =  $180 - \theta$

$$I_o = I_w + I_u \quad (\text{Phasor sum}) \quad (\text{Fig 2})$$

$$I_o = \sqrt{I_w^2 + I_u^2} \quad (\text{Magnitude form})$$

We cannot make  $I_o = 0$   
 because by making  $I_o = 0$   
 the working flux = 0  
 and T/F will not work

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Magnetic Motive force

$$\text{MMF} = \Phi R$$

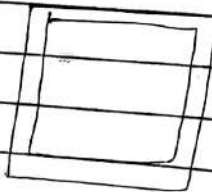
R = Reluctance

$$NIu = \Phi R$$

$$\Phi = \frac{NIu}{R}$$

Use the core of low reluctance

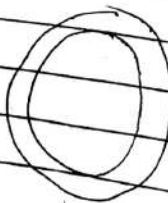
So then we can reduce  $R \downarrow \Phi \uparrow$   
So that  $\Phi$  will remain same.



$$R = \frac{l}{\mu A}$$

How to increase reluctance by decreasing area at core corners

Solution:



Jaws of clamp meter.

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As  $R \gg \eta$

so tell the manufacturer use more no. of turns

### EXAMPLES:

1:

A ring core type CT has a ratio of 2000/20 when operating at a rated primary current with a secondary burden of non-inductive resistance whose value is  $2\Omega$ . ( $Z_L = 2\Omega$ )  $\Rightarrow \delta = 0$ . Takes a no load current ( $I_0$ ) of 2A at power factor of 0.3. Calculate ratio error and phase angle error at full load.

$$n I_s = 2000$$

$$I_s = 10$$

$$n = \frac{2000}{10} = 200$$

2000/10A  
Maximum

$$\delta = 0$$

$$R = \frac{\eta + I_w \cos \delta + I_w \sin \delta}{I_s}$$

$$R = \frac{\eta + I_w}{I_s}$$

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P.f = 0.3

cos β = 0.3

β = cos⁻¹ 0.3

β = 72.54°

I<sub>u</sub> = I<sub>0</sub> cos(90 - β) = 1.908A

I<sub>w</sub> = I<sub>0</sub> cos β =

R = 200 + 2 x 0.3 / 10

R = 200.06

θ = (I<sub>u</sub> x 180) / (η I<sub>s</sub> π) = (I<sub>u</sub> cos δ - I<sub>w</sub> sin δ x 180) / (η I<sub>s</sub> π)

φ = cos(0.3) =

I<sub>u</sub> = I<sub>0</sub> sin β ⇒ θ = 0.05966°

Q If said half load so I<sub>s</sub> = 10 = 5A

%RE = (η - R) x 100 / R

= 0.03%

Ratio Error

one said to find actual phase angle so sub from 180

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Exple:

A bar type CT has 400 turns in secondary winding. The impedance of secondary solenoid is (2 + j1.5)Ω with the 4A flowing in the secondary, the magnetizing MMF is 80AT ampere turn and iron loss is 1 watt. Determine the ratio error and phase angle error.

Solution:-

N<sub>2</sub> = 1 ⇒ (Bar magnet)

N<sub>2</sub> = 400

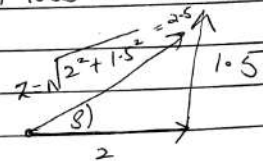
n = N<sub>2</sub>/N<sub>1</sub> = 400

Z<sub>s</sub> = (2 + j1.5)Ω = √(2² + 1.5²) = 2.5Ω

I<sub>s</sub> = 4A

MMF = 80AT

Iron loss = 1 watt



cos δ = 2 / 2.5 = 0.8

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$$\sin \theta = \frac{1.5}{2.5} = 0.6$$

$$\text{MMF} = N_1 I_u = 80$$

$\Rightarrow I_u = 80 \text{ A}$  (MMF is due to  $I_u$ )

$I_w$  is responsible for core losses ( $R_o$  represent core loss)

$$\text{iron loss} = I_w^2 R_o = I_w \cdot I_o R_o$$

$$1 = I_w E_p$$

$$I_w = \frac{1}{E_p} \quad (\text{Now finding } E_p)$$

For finding  $E_p$  finding  $I_s$

$$E_s = I_s \cdot Z_s = 4 \times 2.5$$

$$E_s = 10 \text{ volts}$$

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$$E_p = \frac{E_s}{n} = \frac{10}{400} = \frac{1}{40}$$

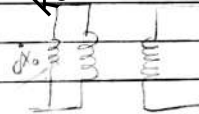
$$E_p = \frac{10}{40} \text{ volts}$$

$$I_w = \frac{1}{1/40} = 40 \text{ A} \Rightarrow I_w = 40 \text{ A}$$

$$R = 420 \quad n = 400$$

$$\% \text{ ratio error} = -4.7\%$$

$$\theta = 1.43^\circ$$



$$R = \frac{400 + 40 \times 0.8 + 80 \times 0.6}{4} \quad \text{series = ?}$$

What is  $jX_o = ?$

$$R = 420.2$$

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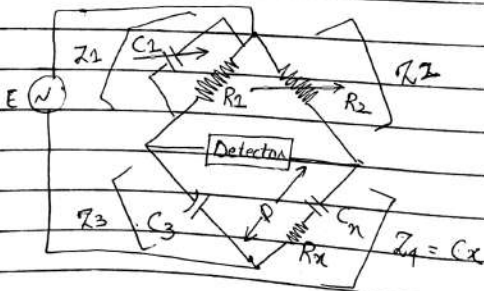
### Lecture

#### Schering Bridge:-

The Schering bridge, one of the most important ac bridges used for measurement of

- Capacitors
- Insulating properties i.e. for phase angles very nearly 90°

$\epsilon_1$  = density of insulating material



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$$Z_1 = \frac{1}{R_1}$$

$$Z_2 = R_2$$

$$Z_3 = ? = -j$$

$$Z_1 = R_1 + j\omega C_1$$

$$= \frac{R_1 + j\omega C_1}{R_1}$$

$$Z_4 = R_4 + \frac{1}{j\omega C_4}$$

$$Z_x = Z_2 Z_3 Y_1$$

$$Z_1 Z_4 = Z_2 Z_3$$

$$\frac{R_x - j}{\omega C_x} = R_2 \left[ \frac{-j}{\omega C_3} \right] \cdot \left[ \frac{1}{R_2} + j\omega C_1 \right]$$

$$\frac{R_x - j}{\omega C_x} = \frac{R_2 C_1}{C_3} - \frac{j R_2}{\omega C_3 R_2}$$

$$\Rightarrow R_x = \frac{R_2 C_1}{C_3}$$

$$\Rightarrow C_x = \frac{C_3 R_1}{R_2}$$

Power factor: PF of a series RC combination is defined as the cosine of the phase angle of the circuit. Therefore PF of the unknown equals

$$PF = \frac{R_x}{Z_x} = \cos \phi$$

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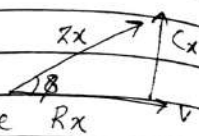
If  $\phi = 90^\circ$

$Z_x =$  Purely capacitive  $R_x$

If  $\phi = 0^\circ$

$Z_x =$  Purely resistive

$0^\circ < \phi < 90^\circ$  (In between behaviour)



Quality of Capacitor depends on resistance of capacitor

$$Q = \frac{\text{Energy stored}}{\text{Dissipated}} = \frac{C}{R_x}$$

D = Dissipation factor

$$D = \frac{1}{Q} = \frac{R_x}{X_c} = \omega C R_x$$

$$D = \omega R_2 C_2 \quad \omega = 2\pi f$$

$C_2$  should impact quality of unknown capacitor  $C_x$ .

$$D = 2\pi f R_2 C_2$$

$\swarrow$   
const.

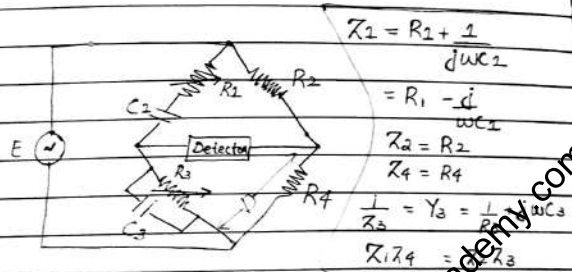
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Unbalance conditions: - (Exple 5.5)

### WHEATSTONE BRIDGE



$$Z_1 = R_1 + \frac{1}{j\omega C_2}$$

$$= R_1 - \frac{j}{\omega C_2}$$

$$Z_2 = R_2$$

$$Z_3 = R_3$$

$$\frac{1}{Z_3} = Y_3 = \frac{1}{R_3} + j\omega C_3$$

$$Z_1 Z_4 = Z_2 Z_3$$

Wien bridge is used

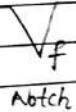
→ for measuring frequency ac bridges

→ as a notch filter in harmonic distortion analyzer.

- as the frequency-determining element in audio and HF oscillators.

Notch filter (Passes a particular frequency through it)

Gang Capacitors (coupled)



Notch

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$R_2$  (mechanically coupled)

$R_4$

$R_2 = \text{Fix ratio} = R$

$R_4$

$$R_2 = 2R_1 \quad (5-52)$$

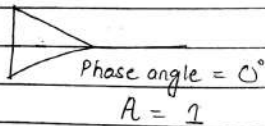
$$R_1 = R_3 = R$$

$$C_2 = C_3 = R$$

Shock in winter is due to stray capacitance

Wagner Ground Connection:

For oscillator gain should be 1.



Google It:

Wein Bridge in Op-Amp

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(Sun January)

If unknown resistance is less than  $1\Omega$  wheatstone bridge is not good solution due to lead resistances (Solution is Kelvin bridge)

For high resistance measurement we cannot use wheatstone bridge (because of sensitivity of detector)

$R \uparrow \quad V \downarrow$

For this problem we use amplifier  
a) Leakage current on surface of insulator  $\epsilon$  can be affected by humidity & temp.

For this we use guard wheatstone bridge.

For Inductor (Maxwell Bridge)

$$1 \leq Q \leq 10$$

$$\text{If } Q \leq 1$$

Desauty bridge

Register

## WAGNER GROUND CONNECTION:

Stray capacitances exist in AC bridges. It exist between bridge element and ground. Do not exist physically but exist electrically

$$X = \frac{1}{2\pi f C}$$

$f \uparrow \rightarrow X \downarrow$   
 $C \uparrow \rightarrow X \downarrow$

x) If we increases  $f \uparrow$  (we take affect of stray capacitances when frequency is very high) = ?  
 becoz  $X \downarrow$  current will move to ground

We can reduce the affect of stray capacitances

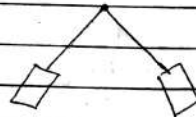
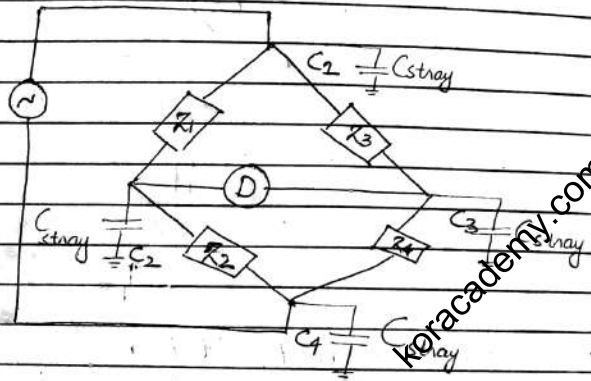
1) Shield the arms of bridge and ground each of the shield. By doing this value of stray capacitance will get constant.

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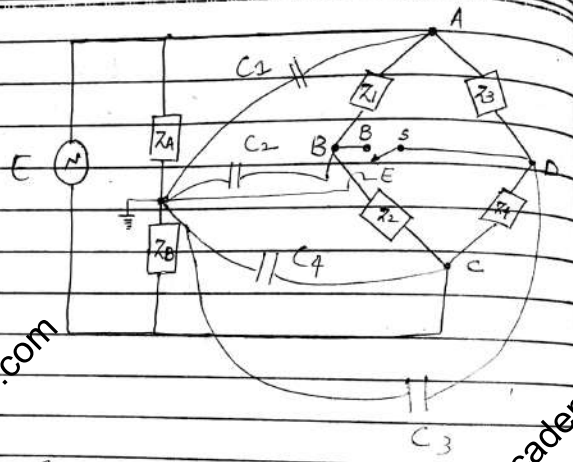
The best solution for solving this problem is Wagner's ground connection.



Two conductors  
 $\epsilon$  in b/w  
 di-electric  
 is capacitor

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STEPS:-

- 1) Connect switch to Pt B and balance the bridge with the help of  $Z_1, Z_2, Z_3$  and  $Z_4$
- 2) Connect switch to pt E and balance the bridge with the help of  $Z_A, Z_B, Z_3,$  and  $Z_4$

It is possible that we change value of  $Z_3$  and  $Z_4$  to check it we have to repeat step 1 again.

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again again

We have to do step 1 & 2 unless the bridge is balance at both B and E for same values of impedances.

That it is my claim that there will be no effect of stray capacitances.

- 1 Step implies  $V_D = V_B$
- 2nd step implies  $V_D = V_E = V_B$

$C_4$  is parallel to  $Z_B$   
 $C_1$  is parallel to  $Z_A$  } neglect its effect

Disadvantage is balancing is time consuming & very difficult.

The best solution is shielding.

Bar Register

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Problem 5.5:-

$$f = 1 \text{ KHz}$$

$$AB : C_1 = 0.2 \mu\text{F}$$

$$BC : R_2 = 500 \Omega$$

CD : unknown

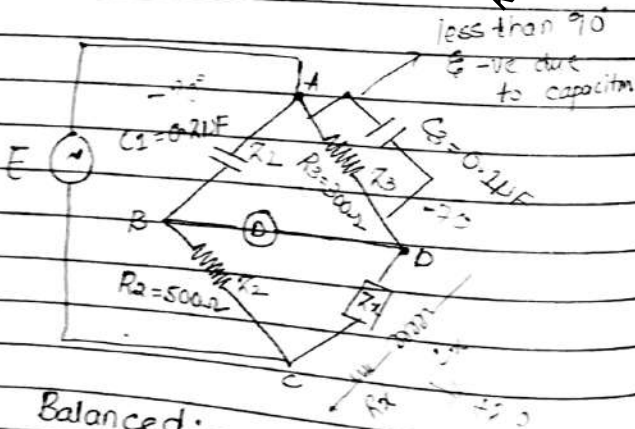
$$DA : R_3 = 300 \Omega // C_3 = 0.1 \mu\text{F}$$

CD: R and C or L



Solution:

First step is to draw the circuit



Balanced:-

$$Z_1 Z_2 = Z_2 Z_3 \quad \text{--- (1)}$$

$$\text{In parallel } Z_x = \frac{Z_2 Z_3}{Z_1}$$

Babar Register

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In parallel we take admittance.

$$Y_3 = \frac{1}{Z_3}$$

$$Z_x = \frac{Z_2}{Z_2 Y_3}$$

$$Z_1 = \frac{-j}{2\pi f C_1} = \frac{-j}{2\pi (1000) (0.2 \times 10^{-6})}$$

$$Z_1 = -j 795.8 \Omega$$

$$Z_2 = R_2 = 500 \Omega$$

$$Y_3 = \frac{1}{R_3} + j 2\pi f C_3$$

$$Y_3 = \frac{1}{300} + j 2\pi (1000) (0.1 \times 10^{-6})$$

$$Y_3 = (3.33 \times 10^{-3} + j 628.32 \times 10^{-6}) \text{ S}$$

$$Z_x = 500$$

$$\frac{(-j 795.8)(3.33 \times 10^{-3} + j 628.32 \times 10^{-6})}{j 628.32 \times 10^{-6}}$$

$$Z_x = (34.4 + j 182.2) \Omega$$

Babar Register

$$Z_x = R_x + j2\pi f L_x$$

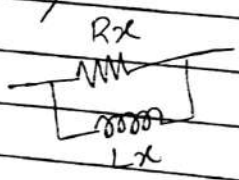
$$R_x = 34.4 \Omega$$

$$2\pi f L_x = 182.2$$

$$L_x = 29 \text{ mH}$$

Question:

Asked unknown adm is in parallel (Rest is same question)



$$Y_x = \frac{1}{Z_x}$$

$$Y_x = G_x - jB_x$$

$$Y_x = \frac{1}{R_x} - j \frac{1}{2\pi f L_x}$$

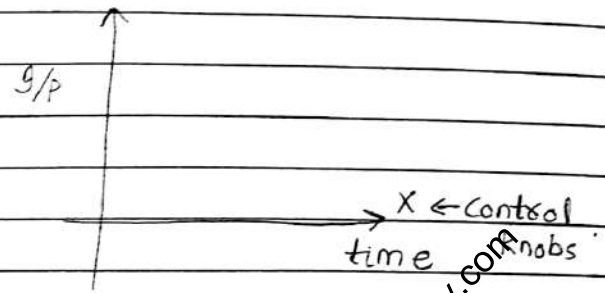
$R_x, L_x$

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## Lecture OSCILLOSCOPE

Oscilloscope give X-Y plot

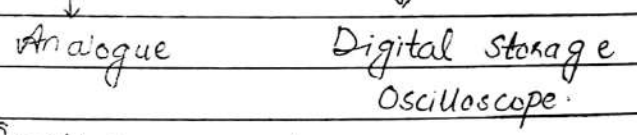


Knob for magnification attenuate.

Oscilloscope functions

- Display
- Measure
- Analyze

Cathode Ray Oscilloscope



Oscilloscope parts:

Cathode Ray tube: It works on the principle of thermionic emission.



Barium Oxide produces more  $e^-$  when it is heated.

Astigmatism:

Graticule (calibrated scale) is pasted outside oscilloscope.

Time base generator produces saw-tooth waveform.



# LAST LECTURE

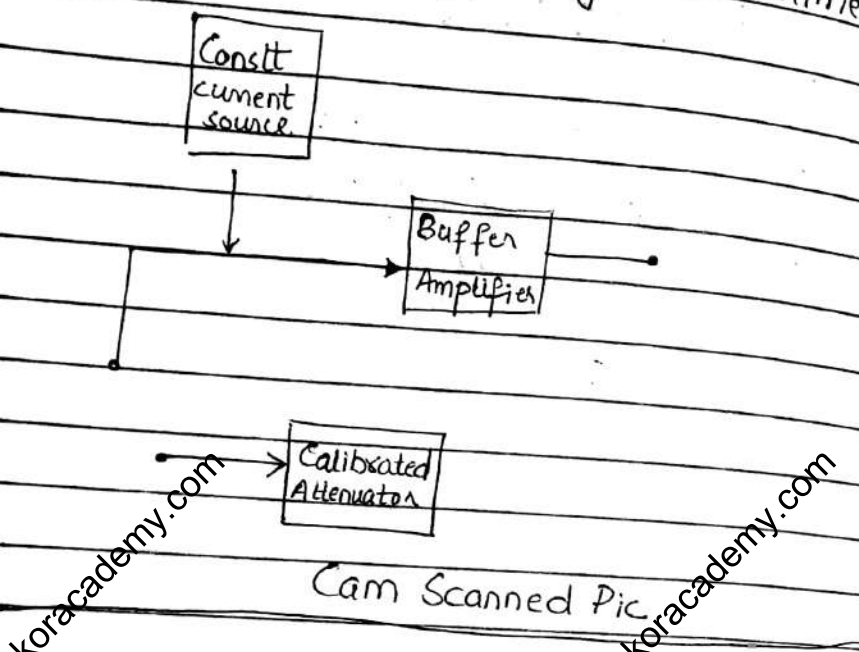
## DIGITAL MULTIMETER:

We will study multimeter to measure 5 quantities:

Principle of operations is that AC voltage, current, resistance & DC other than AC DC voltage. We will convert all these quantities to equivalent DC voltage. We will measure that DC voltage and by calibration we will find that unknown quantity and then we will display it.

- V ~ AC voltage
- V = DC voltage
- A ~ AC current
- A = DC current
- $\Omega$  → resistance.

Block diagram of digital multimeter:-



DC VOLATGE MEASURMENT:

→ Keep Rotary switch to  $V_{DC}$

Calibrated Attenuator will convert high voltage to low voltage as ADC, MC cannot withstand high voltage.

Calibrated attenuator can be consider as series resistance. A lot of voltage will appear across series resistance &

less voltage will appear across MC.

Controller will know the table inside ADC.  
ADC table

1mV	000001000
1.1m	

MC will search in this table and will find voltage at the input of ADC and MC also knows that calibrated attenuates how many times attenuates voltage and will multiply with the factor to get actual voltage.

→ by Noman

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ADC converts to bits.  
Other quantities we will convert to DC voltage and then we will find the known quantity.

If we want to measure small voltages so then we will replace calibrated an attenuator by amplifier.

### AC Voltage measurement

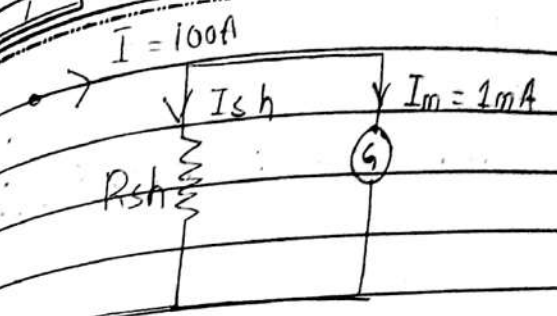
Move the rotary switch to V<sub>n</sub>.

- First calibrated attenuator
- Precision AC to DC converter (Rectifier)
- ADC
- Decoder on UC
- LCD

### DC Current Measurement:

First Convert Current to Equivalent DC Voltage

→ A lot of current will pass through shunt & less current will pass through UC.



$$I_{sh} \approx I$$

$$V_{shunt} = I_{sh} R_{sh}$$

$$V_{shunt} \approx I R_{sh}$$

Vshunt & I (It will produce voltage in parallel proportional to current)

Shunt is very small resistance in mΩ.  
If  $R_{sh}$  is less so voltages  $V_{sh} \downarrow$  less so no need of attenuation of signal.

$$I = \frac{V_{shunt}}{R_{shunt}}$$

Shunt bypass almost current.  
In place of it we can use current to voltage h

### RESISTANCE MEASUREMENT:

Move switch to  $\Omega$  position.

Constt Current source will provide DC current. That DC current will flow through unknown resistor and voltage will appear across it.

### Difference b/w Current Source & Voltage Source:

Generators are voltage sources.

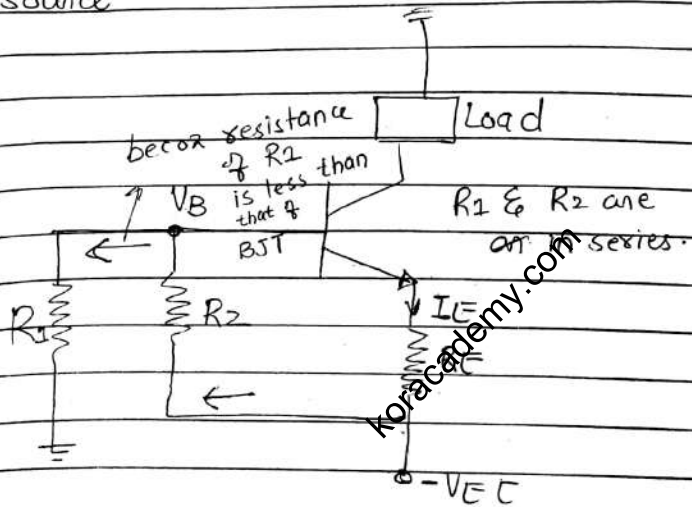
If ~~we inc voltage~~  $V_{in}$  is

If voltage of source is independent of load then the source is voltage source.

If current provided by source is not changing by changing the load so it is a current source

Unknown resistor will act as a load.

How we design a current source



Base I/P impedance of BJT is much larger than  $R_1$  &  $R_2$

$$V_B = \frac{R_2}{R_1 + R_2} (-V_{EE})$$

$$V_{BE} = V_B - V_E = 0.7V$$

$$V_E = V_B - 0.7$$

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$V_{EE} = \text{constt}$  (Constt voltage source)  
 $R_1 \& R_2 = \text{constt}$   
 $V_B = \text{constt}$   
 $\beta = \text{constt}$

$\Rightarrow V_E = \text{constt}$

$I_E = \frac{V_E + V_{EE}}{R_E}$

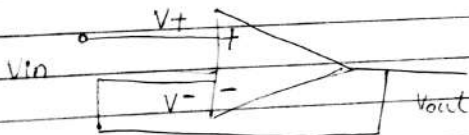
$V_E = \text{constt}$      $V_{EE} = \text{constt}$   
 $R_E = \text{constt}$

$I_E \Rightarrow I_E = \text{constt}$

$I_E \propto I_C$  Acting

so  $I_C = \text{constt}$  (Constt current source)

### Buffer Amplifier:



Gain = 1

Use for impedance matching

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-ve feedback property

$V^+ = V^-$  (Virtual ground) concept

-ve feedback will force op-Amp to have same potential at  $V^+$  &  $V^-$

i.e.  $V^+ = V^-$

feedback will force op-Amp to have same potential at  $V^+ = V^-$

$V^+ = V_{in}$

$V^- = V_{out}$

$V_{out} = V_{in}$

$A_f = 1$

Buffer Amplifier provides two advantages:

- 1) They provide impedance matching.
- 2) Isolation (It isolate one part of ckt from another)

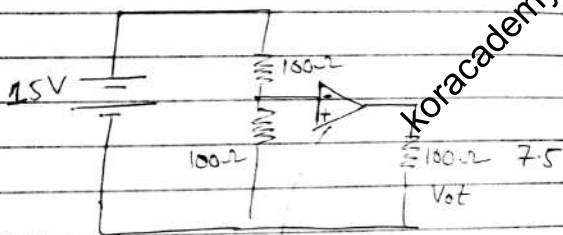
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As Input impedance of Buffer Amplifier is  $\infty$  (infinite) so current will pass through unknown resistance & minimum or no current will pass through Buffer Amplifier. & voltage drop across that unknown resistor.  $[V_a = V_{drop} \propto I]$

Advantage of Buffer Amplifier: -



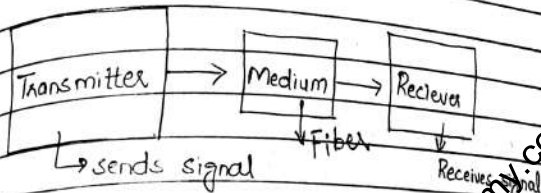
In presence of Buffer amplifier same voltage i.e. 7.5 volt will appear i.e. 7.5V

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## F1 FIBER OPTIC MEASUREMENT:

Three main parts of communication system



Transmitter has to change the form of information so it can travel through the medium (fiber)

Medium  $\rightarrow$  Fiber

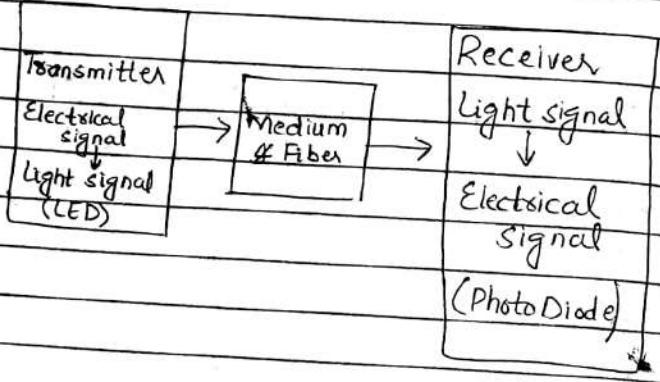
signal  $\downarrow$  light can travel through

Fiber  $\rightarrow$  light can travel through fiber.

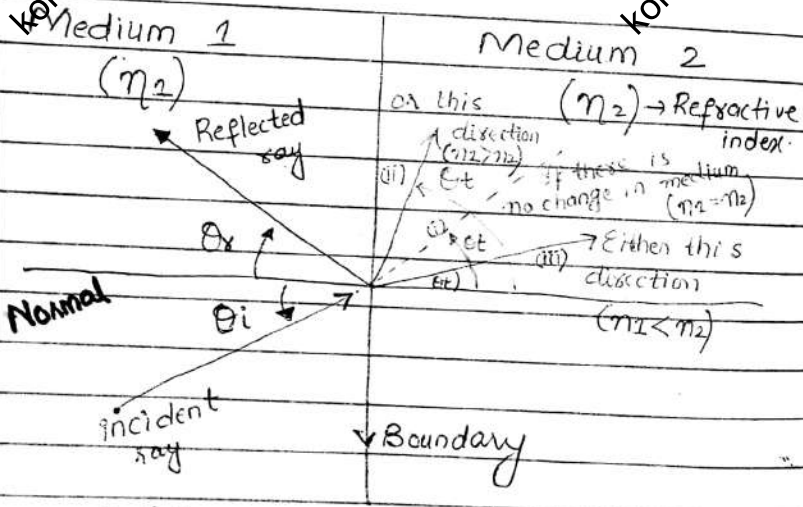
LED converts the electrical signal to light signal.

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Fiber optic works on the principle of total internal reflection



$n$  (Refractive index) of air is equal to one. & for other mediums

$$n > 1$$

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$$i) \quad n_1 = n_2$$

Snell's Law of Reflection:

$$\theta_i = \theta_r$$

Snell's Law of Refraction:-

$$n_1 \sin \theta_i = n_2 \sin \theta_t \quad (2)$$

$$i) \quad n_1 = n_2, \theta_i = \theta_t$$

$$ii) \quad n_1 > n_2$$

According to Snell's law of refraction

$$\sin \theta_i < \sin \theta_t$$

$$\Rightarrow \theta_i < \theta_t$$

So the refracted ray (transmitted) will bend away from the normal.

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iii)  $n_1 < n_2$

$$\sin \theta_i > \sin \theta_t$$

$$\Rightarrow \theta_i > \theta_t$$

When  $n_1 > n_2$

$$\theta_i \uparrow, \theta_t \uparrow$$

When  $\theta_t = 90^\circ$

$$\theta_i = \theta_c$$

Critical angle ( $\theta_c$ ):-

The incident angle at which  $\theta_t$  become  $90^\circ$  is called critical angle.

### TOTAL INTERNAL REFLECTION:

When  $\theta_i > \theta_c$

so the total ray will be reflected and no part of ray will be transmitted.

This phenomenon is use in fiber fiber.

For long range communication fiber is made up of glass

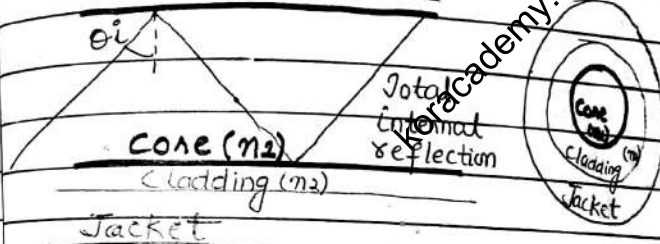
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For short range we uses plastic.

For medium range mixture of glass & plastic is use.

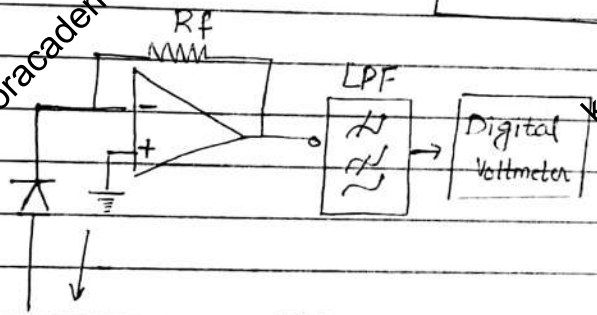
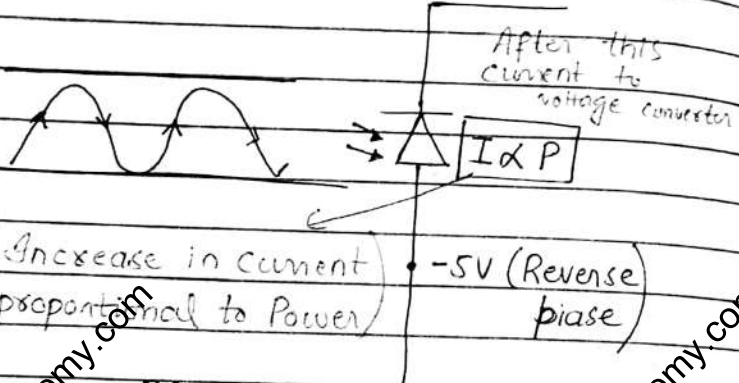
### OPTICAL FIBRE INTERNAL STRUCTURE:-



In medium at different points we use repeaters. (Shape of signal will be recover)

In fiber optic we need less number of repeaters.

## POWER OF THE SIGNAL: (Light Signal)

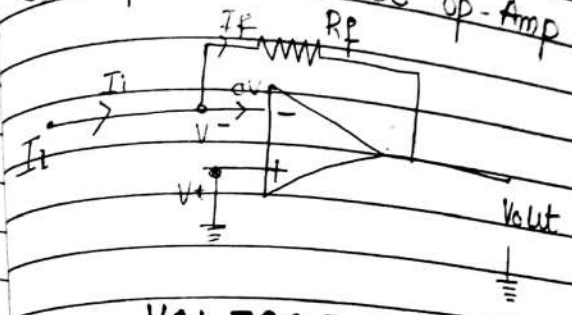


Trans-Impedance Amplifier (Convert current to voltage)

Current to voltage converter should have following two properties:-

- i)  $V_{out} = K I_i$  (resistor also give this property)
- ii)  $V_{out}$  should be independent of load.

Resistor don't give this property. Therefore we use op-amp



## VOLTAGE DIVIDER VOLTAGE TO CURRENT CONVERTER

-ve fb

$$V^- = V^+$$

$$I_f = I_i$$

$$0 - V_{out} = I_f R_f$$

$$V_{out} = -I_i R_f$$

$$K = -R_f$$

$$V_{out} = K I_i$$

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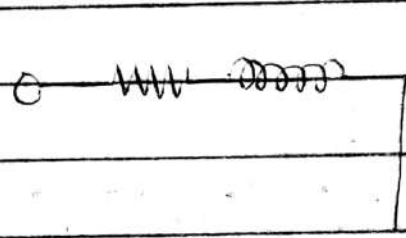
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Due to known reasons these will be noise & noise is in a high frequency component & therefore we use LP filter.

CT:

$$\eta = \frac{I_p}{I_s} \text{ (Nominal ratio)}$$



Leakage flux &  
working flux

EXAMPLE